Microscopic determination of remaining oil distribution in sandstones with different permeability scales using CT-scanning

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Abstract

To investigate the characteristics of oil distribution in porous media systems during a high water-cut stage, sandstones with different permeability scales of $53.63 \times 10^{-3} \mu\text{m}^2$ and $108.11 \times 10^{-3} \mu\text{m}^2$ were imaged under a resolution of $4.12 \mu\text{m}$ during a water flooding process using X-ray tomography. Based on the cluster-size distribution of oil segmented from the tomography images, and through classification using the shape factor and Euler number, the transformation of the oil distribution pattern in different injection stages was studied for samples with different pore structures. In general, the distribution patterns of an oil cluster continuously change during water injection. Large connected oil clusters break off into smaller segments. For sandstones with higher permeability, which show the largest change in distribution pattern, and the remaining oil is trapped in the pores with a radius of approximately $7\text{-}12 \mu\text{m}$. Meanwhile, some disconnected clusters merge and lead to a re-connection during the high water cut period. Whereas the pore structure becomes compact and complex, the residual non-wetting phase becomes static and is difficult to move, and thus all distribution patterns coexist during the entire displacement process, and are mainly distributed in pores with a radius of $8\text{-}12 \mu\text{m}$. For the pore-scale entrapment characteristics of the oil phase during a high water cut period, different enhance oil recovery (EOR) methods should be considered in sandstones correspondent to each permeability scale.

Keywords: X-ray computed microtomography, Remaining oil distribution, Patterns of oil cluster, Pore-scale imaging, Pore network model

1. Introduction

Residual oil in the swept zone of displacement is often taken as the target oil for enhanced recovery processes [1, 2]. During the high water-cut stage, it is difficult to further improve the already high sweeping volume, and therefore the improvement of oil displacement efficiency has become an issue for water injection oil fields. The multi-scale oil displacement mechanism in rocks with different scales of permeability should be considered to provide theoretical guidance with regard to EOR methods and adjustment strategies in high water cut reservoirs, particularly the

microscopic distribution law of the remaining oil clusters [3]. Researchers used fractal and history matching methods to predict the parameters [4-6]. What's more, researchers also used NMR methods to quantitatively study the residual oil distribution and pore size distribution using different NMR T2 spectrums [7-10]. Research has shown that porous systems containing remaining oil are significantly influenced by the pore scale entrapment characteristics of the oil phase [11, 12].

With advances in X-ray tomography (μ CT) and increases in computational power, μ CT has become an excellent technique for the non-destructive capturing of 3D images of the pore structure of reservoir rocks and the residual fluids within them at a resolution of a few microns [13-15]. Owing to a limited description of the connectivity of the pore space, a 2D model is an insufficient representation of the flow behavior, and detailed information extracted from CT images of rocks can be used to accurately study multiphase flows in consolidated and unconsolidated porous media under specific conditions [16, 17]. Starting with glass bead packs [18, 19], researchers tend to test real reservoir rocks and create a more realistic experimental environment. In previous work, researchers obtained the images of real rock systems after both a non-wetting phase injection (drainage) and a wetting phase injection (imbibition) [20-22]. Simulation and experimental examination of the pore-scale multiphase flow behavior has focused on the relative permeability [23, 24], fluid distribution [25-29], capillary pressure measurements [30, 31], oil recovery [32-34], stress sensitivity [35-37], wettability [38-41], and etc.

The morphology, configuration, and migration of the remaining oil clusters during the high water cut stage are of significant importance for oil field development. Therefore, a thorough understanding of the micro-scale distribution properties of the remaining oil in pore space and the changes in such properties based on the permeability scale is critical. Several measurements of the oil cluster distribution have been conducted. In the earliest studies, residual oil clusters of all size were observed as approximately power-law distributions [42]. The cluster size has been found to range from single- to multiple-pore configurations [27, 34, 43]. The size of an oil blob is directly related to the viscous force required to remove the blob, and the blob surface area and volume have an impact on the mass transfer characteristics of the system [44]. Research has shown that a complex pore structure with different scales of permeability is responsible for trapping a large portion of the oil phase within the rock porous spaces. Moreover, a tendency toward an increase in residual non-wetting-phase saturations as the porosity decreases has been noted. This is related to a strong relationship between the trapping and aspect ratio [26]. However, the trapped oil has been measured in pore-scale experiments, these do not reveal the morphology or distribution changes of a trapped cluster in sandstones with different scales of permeability.

The objective of this work is to characterize the pore-scale distribution law of the remaining oil during a high water cut period in sandstones using 3D micro-computed tomography (μ -CT). Two relative homogeneous sandstone samples of different scales of permeability were selected as representative of the different reservoir sandstone systems. We imaged the sequences of the water flooding production steps to elucidate more clearly the changes in the remaining oil distribution and improve our fundamental understanding through which it will be possible to reduce the oil saturation further.

2. Experimental section and methodology

2.1 Sandstone and fluids

We chose two relatively homogeneous sandstone samples with different permeability to model

the different types of porous media. The gas permeability of the two rock samples were $53.63 \times 10^{-3} \mu\text{m}^2$ and $108.11 \times 10^{-3} \mu\text{m}^2$, respectively. The physical properties of the samples used in this investigation are shown in Table 1. To obtain higher-resolution images, cylindrical core plugs were drilled with a diameter of 9.5 mm and length of 25–29 mm.

Table 1 Physical properties of the sandstone samples.

Number	Permeability ^a ($\times 10^{-3} \mu\text{m}^2$)	Porosity ^b (%)	Small core plugs		
			Length(mm)	Diameter(mm)	Porosity ^c (%)
1	108.11	21.12	25.5	9.4	20.88
2	53.63	22.31	26.5	9.4	23.02

^a Measured at 297.15K using nitrogen.

^b Measured at 297.15K using nitrogen.

^c Measured at 297.15K using water.

Brine (salinity of 7850 mg/L) doped with 10 wt.% potassium iodide (to enhance the CT contrast) was applied as the aqueous phase, and crude oil mixed with 52.1 wt.% kerosene was used as the oil phase. The viscosity of the aqueous phase is 1.2 mPa·s, whereas that for the oil phase is 8.9 mPa·s.

Table 2 Composition of Brine

Salinity (mg/L)	SO_4^{2-} (mg/L)	Cl^- & I^- (mg/L)	Mg^{2+} (mg/L)	Ca^{2+} (mg/L)	Na^+ & K^+ (mg/L)
7850	800	3500	20	30	3500

2.2 Experimental setup and procedure

The experimental installation comprises four main parts: a core holder, X-ray micro CT equipment, a pumping system, and intermediate containers. The core holder sleeve is made of polyetheretherketone (PEEK), whereas the inlet and outlet end plugs are made of stainless steel. The fluids were injected into the horizontally positioned plug using standard pumps. X-ray micro-tomography was used to scan the pore structure and map the distribution of oil clusters during the water flooding process.

Fig. 1 shows a schematic sequence of the experimental procedure. All experiments were conducted at 297.15 K and atmospheric pressure (0.1 MPa). Initially, the samples were scanned dry to obtain an accurate mapping of the pore structure. Then, the cores were completely saturated with brine under vacuum, and an approximately 200 pore volume (PV) of oil was injected until the water production ceased. After aging, the cores were scanned again to obtain the distribution of oil phase under a connate oil saturation (S_o) state. During stage IV, the core plug was water-flooded at a velocity of 0.1 ml/min, and μ -CT images of the cores at 1, 5, 15, and 50 PV injection stages were then acquired. As the CT data could be more accurate and easily segment while the core reaches the static condition (no flow), the pump and the pressure valves on both ends of the core holder were turned off and allowed to stand for 1 h before each scanning. We took the image quality as the standard to determine the stable state of core samples in this experiment, especially the interface between different phases. A quick scan test with low resolution but short time-consuming can be used to evaluate if the holder was ready to be imaged. If the distribution of fluid phase in pore space achieves stability, the captured interface should be very clear with the naked eye and easy to be

segmented. Then CT images with high resolution can be acquired under static condition.

In brief, multiple scanning cycles were applied for the plugs, and we obtained five groups of CT images. The sandstone cores were imaged at a resolution of $4.12\ \mu\text{m}$ in all directions at different displacement stages, and the main scan area was the central region of 3.7 mm in diameter. The imaging was applied at approximately the middle part of the column to fix the location and avoid the boundary effects on the spatial distribution and configurations of immiscible fluids.

Fig. 1 Schematic sequence of the experimental procedure (S_{wc} : irreducible water saturation; S_{or} : residual oil saturation)

Fig. 2 A simplified schematic diagram of the displacement experiment based on CT scanning

2.3 Image processing

To correlate the characteristics of the pore structure of different scales of permeability and oil distributions quantitatively, significant processing needs to be applied to the raw CT images. First, noise must be removed from an extracted portion ($300 \times 300 \times 300$ pixels) of the raw images using a non-local means filter [45, 46], which can increase the signal but does not increase the interface width from the raw images.

Prior to any analysis, the gray-scale CT images must be segmented into binary images based on the intensity value of each phase and the histogram of the gray-scale values. Segmentation is the essential process of uniquely identifying different phases in the images based on their different levels of X-ray absorptivity, which means each phase has a range of intensity values. Images containing a partial saturation of multiple fluids are significantly more difficult to segment than dry images [47]. However, in this study, we used a watershed algorithm, which is quite versatile and can be applied to multiphase images [35]. The process of determining the threshold is typically

combined with a recognition of the peaks within a gray-scale histogram (Fig. 3) [48]. The accuracy of the segmentation was verified by comparing the results obtained from the segmented images with the experiment results. All raw CT images were filtered and segmented within the commercial software package Avizo (FEI Visualization Sciences Group). Note that, for each process step, the same areas were compared. Fig. 4 shows slices through the rock during the water flooding experiment.

Fig. 3 Histogram of the different grey-scale values for CT images (left: sample with multiphase-fluid; right: dry sample)

Fig. 4 Image processing procedure (left: raw CT images, middle: the filtered images, right: the corresponding segmented image. Oil: black, brine: dark grey, rock: light grey, resolution: 4.12 μm)

2.4 Pore space segmentation

A binary image space can be defined as a set of points, which are often called voxels in 3D imaging. According to morphological theory, the distance transformation, which is represented by a distance map, is widely used in image analysis and segmentation [49]. A distance map is a gray-level image where the value of each point of pore space (object point) corresponds to its shortest distance to all matrix points (background points). Some of the more common distance functions include the Euclidean distance, city-block distance, and chessboard distance, the most accurate of which is the Euclidean distance. The Euclidean distance is calculated by linking two points using a straight line [50]:

$$d_E(p, q) = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2 + (z_1 - z_2)^2}$$

Where $d_E(p, q)$ is the Euclidean distance between points p and q , and x , y , and z are the coordinates of the points.

In this study, a distance-map based method was used to determine the pore size and distribution for analyses of the pore structure and remaining oil distribution (Fig. 5). Combining the Euclidean

distance map and watershed algorithm, each pore space can be segmented and located by distinguishing the “basin” and “peak” areas [51]. Then, the pore radii were obtained using the radius of the max ball of each pore.

Fig. 5 Euclidean-processing workflow (left: binary image; middle: Euclidean distance map; right: segmentation of pore space)

2.5 Connectivity of pore space

The pore network model (PNM) is now able to represent the complex topological structure of the pore space more adequately [52]. By simplifying a realistic pore space such as spheres and cylinders, research into the quantification of the pore structure and pore-scale transport mechanism can be conducted [53]. This approach allows us to map the pore structure and determine the connectivity of the pore space from high-resolution images [54].

The connectivity function $E_V(r)$ is a global description of the topological properties. It can easily be determined for the network model by [55]

$$E_V(r) = \frac{N_n(r) - N_b(r)}{V}$$

Where $N_n(r)$ is the number of nodes, and $N_b(r)$ is the number of bonds, in which only bonds with a radius of larger or equal to r are considered.

3. Results and discussion

3.1 Pore structure analysis

Table 3 shows cross sections of the two selected porous systems extracted from the CT images. We then extracted a portion ($300 \times 300 \times 300$ voxels) of the raw CT images for segmentation and analysis using the pore network model and distance transformation [56, 57]. Each volume represented a rectangular portion inside the sample to avoid the boundary effects of the columns.

Table 3 Digital core reconstruction and analysis

Sample No.& Permeability	1# $108.11 \times 10^{-3} \mu\text{m}^2$	2# $53.63 \times 10^{-3} \mu\text{m}^2$
CT images (diameter of the image is 3.87mm)
Connected pores (connected pores were shown in the same color)
Digital core(light blue: pore; dark blue: matrix)
PNM(green: throat; red: pore)
Pore radius frequency distribution curves

From the CT gray-scale and PNM images, we can see that, as the permeability of the samples is reduced, the pore structure becomes complex; medium pores, small pores, and fine throats develop. The distribution of the pore radius can be quantified using the distance-map based method mentioned above, as shown in Table 3. As the permeability and porosity of the samples decrease, the range of pore radius narrows, the peak value moves to the left, and the mean radius and effective porosity decrease. Table 4 lists the parameters of the samples obtained through a PNM characterization under a resolution of $4.12 \mu\text{m}$. As indicated above, the mean pore and throat radii both decrease, although the throat radius changes more than pore radius based on the peak of the frequency distribution curve. Moreover, with the decrease in permeability, the mean volumes of the pore and throat decrease, the mean tortuosity shows a tendency to increase, and the intersection of the connectivity function curve (Fig. 6) with the X-axis moves to the left, which means the connectivity of the pore space worsens [55].

Table 4 Parameters of the samples obtained by PNM characterization

Parameters	1#	2#
Number of pores	7593	36187
Mean pore radius (μm)	11.10	6.52
Mean volume of pore ($10^3 \mu\text{m}^3$)	16.5	3.21
Number of throats	13955	67692
Mean throat radius (μm)	7.92	4.88
Mean volume of throats (μm^3)	8.12	2.23
Mean length of throats (μm^3)	25.4	16.00
Mean shape factor	0.0487	0.0545
Mean coordination number	3.64	3.72
Mean Tortuosity	2.36	2.69
Effective porosity (%) ^a	22.81	22.12

^a Effective porosity with resolution of $4.12\mu\text{m}$.

Fig. 6 Connectivity function curves

3.2 Pore-scale classification of remaining oil

To characterize the connected oil clusters in a segmented image, we identify individual clusters and provide each with a unique label based on some first-order statistical information of each voxel's 26 neighboring voxels. Disconnected oil blobs are labeled with distinct numerical values starting from 1 up to the maximum number of individual blobs in the image. The parameters such as the volume, interfacial area, sphericity index, and distribution pattern of every individual oil cluster are then computed by performing operations on these sets of voxels.

Table 5 Quantitative characterization of remaining oil

Distribution pattern	Standards	Typical figure
Network	$G < 0.1$
Branched	$0.1 < G < 0.3$
Multiple	$0.3 < G < 0.7$ & $E \geq 1$
Singlet	$G > 0.7$
Film	$0.3 < G < 0.7$ & $E < 1$

The remaining oil saturation is computed as the ratio of the voxels of the oil phase to the pore space. Once the individual oil blobs are labeled, it is easy to calculate the volume of each oil blob V_{blob} as well as the total oil volume S_o (remaining oil saturation). Several algorithms are available to calculate the interfacial area from a digital core, and their accuracy is primarily a function of the resolution of the images. The interfacial areas were computed using an optimized simple face counting algorithm, which can provide a reasonable estimate based on our high-resolution images. The algorithm calculates the surface area (SA_{blob}) based on the number of areas of the faces of the boundary voxels, and a summation of the distances between each boundary voxel. There are two important parameters used to distinguish the distribution patterns of the remaining oil. One is the sphericity index, which describes how closely an oil blob resembles a sphere, and is computed as follows [58]:

$$G = \frac{6\sqrt{\pi}V}{S^{1.5}}$$

Where S is the surface area of the oil clusters, and V is the volume. For a perfect sphere, $G = 1$.

Another is the Euler number (E), which can be used as a characteristic describing the topological properties of the residual oil clusters. The Euler number can be expressed using three Betti numbers [59].

$$E = b_0 - b_1 + b_2$$

Where b_0 is the number of isolated components, b_1 is the number of tunnels, and b_2 is the number of cavities.

The sphericity index (G) and Euler number (E) are combined such that the distribution pattern of the remaining oil can be defined (Table 5).

Fig. 7 Remaining oil saturation curves

The residual oil saturation decreases with the water flooding (Fig. 7). As the pore structure becomes complicated, the decreasing tendency in the oil saturation slows, and the irreducible oil saturation increases. A three-dimensional visualization of the remaining oil (Fig. 8) during displacement shows that the volume of the remaining oil in the pore spaces is reduced and its distribution patterns are continuously changed.

Sample 1#:

Sample 2#:

Fig. 8 Three-dimensional visualization of remaining oil after different brine PV injections

The volume fraction of each remaining oil pattern during each water-flooding stage was calculated, as shown in Fig. 9. Because a large amount of the remaining connected oil exists in the pore space, the distribution pattern of the oil is mainly in a “network” form during the initial stage. With the processing of the water flooding, the oil clusters are cut off, the volume of the network form continually decreases, and the volume of other forms such as the “branched” and “multiple” forms gradually increase. The specific changing trend of the distribution pattern differs over the pore structures. Moreover, oil distributed in a “film” form is too small to acquire at this experimental resolution, and thus the volume of the film is consistently low and does not change much during the entire displacement process.

Fig. 9 Change of distribution pattern during water displacement

Sample #1, which has better connectivity, showed the largest amount of changes in terms of the distribution pattern of the residual oil. At the saturated oil stage, five types of distribution patterns coexist together. The pattern of “network” occupied nearly 50%, and the other shared 50%. With the process of drainage, “network” decreases rapidly, which could be due to the breakup of the oil phase affected by the snap-off events. Four other distribution patterns of the residual oil coexisted during the entire displacement process. The distribution pattern is mainly in multiple and branched forms after injection of 50 PV of brine. We also observed a transition from a connected oil phase flow of a network form into disconnected clusters, which break off as fragments. During this process, the volume fraction of the connected oil phase continued decreasing, and the number of oil clusters continued increasing. This can also be seen from the fact that the oil volume of branched and multiple forms increases sharply when the oil in a network form decreases rapidly.

Furthermore, a redistribution of the remaining oil can be observed after the injection of 5 PV of brine. The volume of the branched form increased with the decrease in volume of the multiple forms, which may be because of the coalescence.

In contrast, as for Sample #2, which has a more complicated pore structure, water flooding did not work well owing to the effect of the pore structure. Their remaining oil distribution pattern changes less while the distribution of oil clusters becomes more complex. All five distribution patterns coexist during the entire displacement process, and are mainly in network form.

3.3 Remaining oil distribution during high water cut period

Combining the pore space segmentation and reconstruction of an oil cluster, an oil-rich area where oil is retained can be analyzed. For Sample #1, as shown in Fig. 10. The initial oil is mainly saturated in radius from about $5\mu\text{m}$ to $25\mu\text{m}$, its distribution range is similar to the pore radius frequency curve, and most of the remaining oil clusters are distributed in pores with the radius of $8\mu\text{m}$, $12\mu\text{m}$ and $15\mu\text{m}$ rather than large pores with a radius more than $20\mu\text{m}$. After water flooding, we can see the significant change that the remaining oil is mainly distributed in pores with radius from $7\mu\text{m}$ to $12\mu\text{m}$, which indicates the remaining oil in radius over $12\mu\text{m}$ was swept out. During the later period of displacement, a non-uniform displacement can be observed. There was no big change of the oil saturation in a part of pores, meanwhile, the saturation in other pores continues to reduce. Because of flow around a body phenomenon, there are some areas which cannot be swept by the injected water, therefore, a lot of remaining oil is trapped in those pores with a high pore-throat ratio.

Changes in the remaining oil distribution of Sample #2 are shown in Fig. 10. Most of the remaining oil was distributed in pores with a radius ranging between 6 and $19\mu\text{m}$ prior to the water

flooding. As the pore structure becomes more complicated, the swept area of the injected water becomes limited. And pores with a radius ranging between 8 and 12 μm , which abounds in the oil first, still capture a large number of oil clusters. Similar to Sample #1, because an area with a high pore-throat ratio where large pores are encircled by small pores and throats has more potential to trap oil clusters, oil saturation is higher in pores with a radius of 10 μm .

As shown in Fig. 7, the remaining oil saturation of Sample #1 is relatively lower after water flooding. Beside the small oil blobs formed as a singlet or multiple patterns trapped in the swept pores and throats, and also the big oil clusters of branched form usually remained in the large pores (Fig. 9). According to the pore network model, the location with large oil volume can be labelled and analysis. This area, we found that is controlled by the small throats, the large pores trapped with oil has high radius ratio between pores and throats which connected with them, they also have relatively low coordination number and complex shape factor, so that the saturated oil phase was harder to be displaced.

Fig. 11 show the distribution of two sample's remaining oil in PNM (after water flooding). For Sample #1, we can see that the remaining oil has a more concentrated distribution than Sample #2, and mainly at the corner. As for Sample #2, there are much more pores still remains oil, and the pore size is much smaller than Sample #1.

Fig. 10 Radius frequency distribution curves of pores with oil content

Fig. 11 The main corresponding distribution area of remaining oil in PNM (after water flooding, green is throat while red represent remaining oil in pore)

3.4 Remaining oil distribution during water flooding

For the samples with different scales of permeability, there exists a difference in water flooding effectiveness which is also reflected in distribution pattern and location of remaining oil clusters. After a long production history of water flooding, most of the oil in sandstones with relatively high permeability, represented by Sample #1, will be swept, and the remaining oil becomes distributed in multiple and branched form and in pores with a radius of 7–12 μm . However, even in a micro scale experiment, not all pores of high permeability samples can be displaced in the process of water flooding. Rich areas of remaining oil with a high pore throat ratio have little influence under the current stable pressure field. Because the connectivity is poorer than Sample #1, oil clusters in sandstones represented by Sample #2 have local concentrations and global expansion during water flooding. The remaining oil is mainly stuck in pores with a radius of 10 μm in a network form. As for the reason why, the sandstones with low permeability have a low sweep efficiency may relate to the complexity of pore structure, smaller size, and more dispersed pore.

4. Conclusions

High-resolution imaging technology is used to investigate the characteristics of oil distribution in porous media systems during the stage of a high water cut. The findings indicate that the remaining oil distribution is influenced by the pore structure and injected fluid volumes. Because EOR methods for reservoirs containing the remaining oil are greatly influenced by the pore scale entrapment characteristics of the oil phase, this study should result in improvements in our ability to further enhance the oil recovery.

- (1) Low-permeability sandstones were more likely to have smaller pores and poor connectivity, which results in the oil production encountering greater resistance. The residual oil saturation tends to increase as the pore structure becomes more complicated, where large oil blobs are trapped in such systems.
- (2) During imbibition, the volume of the remaining oil reduced, trapping occurs within an appreciable fraction of the total number of pores in the rock. Meanwhile, the distribution patterns of the oil clusters continuously change during the displacement process, there is one dominating oil cluster in a network form during the initial phase, and is broken into other distribution patterns with the water flooding. Cores with good pore connectivity show the biggest changes in terms of the distribution pattern of the residual oil, transitioning from a connected oil phase flow in a network form into disconnected clusters, which break off into fragments, as can be observed during the displacement. The oil volume in a branched or multiple from increases sharply when the network form of the oil decrease during the stage of a high water cut. The residual oil distribution pattern of cores with a compact pore structure shows smaller changes, whereas the oil clusters have a more complex distribution. Because of the low degree of production, all five distribution patterns coexist during the entire displacement process, which is mainly in a network form.
- (3) The initial oil distribution in Samples #1 is mainly in pores with radius range 5-25 μm , while the remaining oil after 50PV is mainly in pores of radius of 7-10 μm . In sample 2#, the initial oil distribution is a Gaussian type shape from 5 to 25 μm pore radius and turns to pluri-modal trend as for sample 1# with pore radius range between 8 and 12 μm .

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