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# Towards robust scenarios of spatio-temporal renewable energy planning: A GIS-RO approach

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**Abstract.** Solar-based energy is an intermittent power resource whose potential pattern varies in space and time. Planning the penetration of such resource into a regional power network is a strategic problem that requires both to locate and bound candidate parcels subject to multiple geographical restrictions and to determine the subset of these and their size so that the solar energy production is maximized and the associated costs minimized. The problem is also permeated with uncertainty present in the estimated forecast energy demand, resource potential and technical costs. This paper presents a novel combination of Geographic Information Systems (GIS) and Robust Optimization (RO) to develop strategic planning scenarios of a collection of parcels that accounts for their spatio-temporal characteristics, and specifically their hourly radiation patterns that are location dependent, to best fit the network temporal demand and minimize technical costs.

The problem is formulated as a GIS spatial placement problem and a RO fractional knapsack problem to plan the effective power penetration and geographical suitability of new PV facilities. The combination GIS-RO generates an excellent decision support system that allows for the computation of optimized parcel scenarios (locations, sizes and power). The qualitative and quantitative effectiveness of the approach is demonstrated on real data on the French Guiana region. Results show that the proposed approach provides reliable fine grained planning that also accounts for the risk adversity of the decision maker towards forecast demand and solar potentials.

**Keywords:** Renewable energy planning · Geographic Information systems · Robust optimization.

## 1 Introduction and related work

Energy transition from a high-carbon regime born of fossil fuels to low-carbon solutions is a major challenge of current societies [10]. Most of the energy planning strategies therefore aim at enhancing the share of renewable energy (RE) sources within power networks [23]. When those energies are dispatchable, the integration remains pretty straightforward [16,36]. However, when it comes to

volatile, or *intermittent* RE sources, this is no longer true. Their unstable and variability nature implies that the resulting aggregated power injected into the grid may threaten network’s stability by not matching the power demand [23].

Thus, the full problem of integrating intermittent RE sources in power networks involves irregular spatio-temporal energy potential patterns, related to the location and dimensions of power facilities. It is a multi-criteria uncertain optimization and planning problem that combines the spatial placement of candidate parcels for installing power facilities subject to *geographical* constraints and *temporal* resource constraints, and the selection (location, size and capacity) of optimal plants such that the power into the network is increased at minimal costs and short-term unpredictability is limited to an acceptable level.

Taking into account spatio-temporal energy potential data, together with heterogeneous land, network, and technico-economic constraints for effective renewable energy planning remains a challenging multi-dimensional problem permeated with uncertain data [37]. The computational approaches are broadly divided into two research streams: 1) geographical information system (GIS) modeling with multi-criteria decision-making (MCDM) [6,13,34,3], and 2) bottom-up engineering approaches [23,35,7,37]. GIS models with MCDM focus on providing suitability maps based on static resource assessment and expert-based decision criteria. The maps depict areas with their respective weighted criteria values to be used in the MCDM model, such as economic, environmental or technical ones. These approaches do not aim at optimizing the actual parcel selection that would require taking into consideration the short-term temporal variation of both the resource and power demand, or their evolution in the long-term. On the other hand, bottom-up engineering approaches allow for time simulation and optimization of given energy system configurations. Their main objective is to guide energy policy road map often at a national scale and longer time horizon. This systemic approach gives a significant insight into the potential contribution of RE sources [12,11], but does not aim at identifying physical parcel locations. Similarly [22] addresses the resource management problem as a knapsack problem, that shows the suitability of linear programming to select among experts’ given parcels, the ones with highest resource potential. It does not consider the hourly temporal patterns of the different sites and their projected uncertainty, the possibility to consider a fraction of a given parcel, nor the impact of geographical restrictions and distances, and the complexity of the associated technical costs.

In summary, to date we are not aware of computational approaches that tackle the spatio-temporal optimization problem consisting of identifying the best parcels that increase solar energy penetration into the network at minimal cost, while satisfying a region’s specific constraints (terrain, resource, infrastructures, etc) and related costs. This paper addresses this problem by proposing a two-steps specification in terms of a spatial placement and a resource planning problem, and we propose an integrated computational approach. The approach contributes a novel framework based on GIS spatio-temporal data and constraint processing, connected to a Robust Optimization (RO) knapsack model to plan

renewable energy scenarios. The combination GIS-RO generates an excellent decision support system that allows for the planning of parcel scenarios (locations and areas) that will best increase the RE power into the network at minimal cost, according to the decision maker risk adversity. A GIS can handle very large volumes of data, including remote sensing images for solar radiation indicators, land use maps, and various networks maps (electrical, roads, water). The application of global and multi-layers geographical constraints and various control parameters allow for an effective deterministic pruning of the region, to determine suitable candidate parcels, and their relevant properties without impairing the optimization problem.

The core contributions of this paper are: 1) the specification of a complex spatial placement and planning problem, 2) a computational approach that efficiently exploits GIS geographical constraints, and makes powerful use of large scale spatio-temporal environmental data, and 3) an integration of the spatial analysis with a robust optimization module through a comprehensive set of resource and contextual features. Through the use of Robust Optimization, data uncertainty present in the forecast figures for the planned horizon is tackled with a measure of robustness, allowing best and worst case scenarios to be studied according to various risk adversity positions of the decision maker.

The GIS-RO framework presented in this paper, is applied to a real world challenge of PV solar power plants planning in the region of French Guiana. It illustrates the qualitative and quantitative efficiency of the approach as a decision support system providing solution scenarios. The paper is organized as follows: Section 2 describes the problem and overall approach; section 3 presents the GIS module; section 4 the robust optimization model; section 5 is the experimental section based on a real-world case study for robust spatial decision making from time series resources; and section 6 concludes the paper.

## 2 Problem description, application and approach

The problem is motivated by a renewable energy scenario planning problem from the 2015 Energy Transition Act. France’s energy policy has the target for overseas regions, in particular French Guiana, of 50 % of renewable energy in final consumption in 2020 and full energy self-sufficiency by 2030 [15]. The challenge is to identify suitable candidate parcels for RE parks and determine the ones, and their optimal size, that would maximize power network contribution at minimal costs. A candidate parcel must satisfy a number of geographical constraints, including topographic land use restrictions, type of ground surface, be at a maximum distance threshold from the electrical grid, and have a maximum surface with limited land slope. These constraints bound the areas for candidate parcels.

The scenarios for the best parcels selection deal with the resource potential and costs associated with each candidate parcel. The intermittent resource follows a temporal pattern specific to the geographic location. The costs are mainly technical costs (installation, maintenance, grid connection) that depend on the size of the parcel and its distance to the grid. These data have a degree of un-

certainty in terms of their future value. The full problem can actually be defined as a spatial placement problem to identify candidate parcels, and a fractional uncertain knapsack problem with forecast time-series resource, to compute scenarios of optimal parcel selection and sizes. This paper aims at defining and showing the strengths of a combined GIS and RO computational approach to tackle complex spatial decision making problems with time-series resources, with application here to solar energy placement and planning.

*Integrated computational work-flow* The work-flow depicted in Fig. 1 best describes the computational process and integration of the two modules. We first describe the main inputs, then each module. Geographical data layers and control parameters input the developed GIS GREECE module, which implements methods to determine the candidate parcels, and contributes a despatialization of the relevant features for each parcel (resource pattern, maximal size and costs), needed to enrich the RO model.

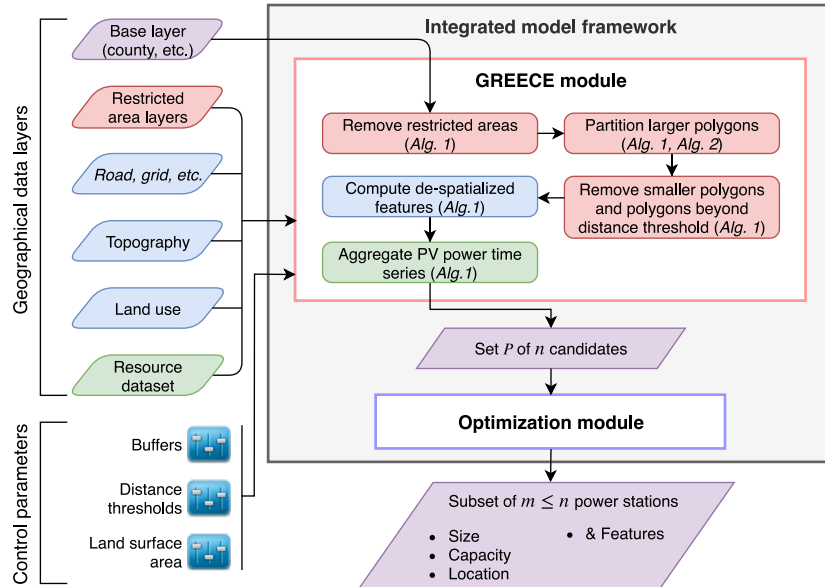


Fig. 1: GIS-RO integrated workflow

*Data, constraints and control parameters* In GIS terminology, the concept of layer corresponds to geographic datasets. When the dataset is an image, the term Raster is commonly used. The geometric objects are in vector mode and can be specified as polygons, lines or points. As depicted in Fig. 1, input data layers correspond to: 1) the study region or base layer, 2) the restricted area layers, 3) specific objects for which distance to resulting polygons must be computed (e.g. road, grid), 4) terrain features (land use and topography) and 5) the resource of interest (here solar radiation maps).

The restricted area layers stand for polygons where facilities cannot or should not be established. Typically, they include urban areas, ecological zones, water-

courses, military sectors, cultural heritage, etc. They may also represent zones too far from specific objects (e.g. electrical grid). Geographic elements for which distance must be computed can be of any kind but are generally related to connection and accessibility costs such as road and grid networks. Topography and land use allow terrain to be characterized within each polygon. Finally, resource dataset is a set of raster or vector processed images, potentially with time series. Data layers and maps are retrieved from national and international geographic databases or remote sensing image processing.

The range control parameters are set by the user, and allow for different land management scenarios to be generated. Buffers surrounding geographic objects depend both on their type and on the kind of power station. Distance thresholds to given layers (e.g. road network, electrical grid) stand for the limit beyond which establishing a facility is not economically viable. Finally, land surface area specify a region's land management in terms of minimum and maximum allowed surface thresholds. Smaller or larger parcels might respectively be excluded from the study, or partitioned into suitable smaller parcels.

### 3 GIS module: GREECE

We specify the Geographical RENEwable Energy Candidate Extraction problem below, then describe our spatial partitioning and placement solution methods.

---

**Given:**

$B_{layer}$	Base layer (i.e. a set of polygons)
$R_{layer}$	Restricted area layers
$D_{layer}$	Distance threshold layers (i.e. sets of geometries)
$h$	Matrix of elevation values (DEM) associated to the base layer
$R_{maps}$	Set of resource raster maps
$LU_{layer}$	Land-use layer
$NET_{layers}$	Layers (e.g. grid, roads, ...) for which distance to each resulting polygon must be calculated
$B_{uffers}$	Control parameter: Set of buffer values, each associated with a given layer
$DistT$	Control parameter: Set of distance threshold values, defined for each $D_{layer}$
$s_{min}, s_{max}$	Control parameter: Surface thresholds

**Find:**

The set  $P$  of candidate parcels

The de-spatialized resource time series and geographical features for each parcel

**Such that the following geographical restrictions hold:**

A candidate parcel is geographically disjoint from all layers of restricted areas

The surface of a candidate parcel is within given bounds

A candidate parcel is within a bounded distance from the threshold layers

---

For space reasons, we give the main procedure in Algorithm 1, the spatial partitioning algorithm, and describe our spatial slicing and extraction methods, developed with Python GIS packages. The general procedure is decomposed in two main steps: 1) spatial placement and partitioning (Alg.1: line 2-10) , 2) conversion of the resulting polygons defined by their geographical coordinates into *de-spatialized* items with relevant features (Alg.1: line 11-20). The set of

relevant built-in Python GIS functions for topological, raster, set and graph operations is defined (packages used: [geopandas](#), [shapely](#), [rtree](#), [gdal](#) [21], [numpy](#) [43], and [networkx](#)).

#### Topological geometric and raster images operators

DISTANCE( $p, P$ )	Minimum euclidean distance between centroid of polygon $p$ and all elements in set $P$
UNION( $p_1, \dots, p_n$ )	geometric union of the polygons $p_i$
RTREEIDX( $P$ )	Compute spatial index $idx$ of all elements in $P$
INTERSECTS( $p, P, idx$ )	geometric intersection of $p$ with elements in $P$
SHAPE( $p$ )	Shape factor of polygon $p$ (e.g. roundness)
SURFACE( $p$ )	Surface of polygon $p$
SLOPE( $h$ )	Slope raster from the Digital Elevation Model $h$
ASPECT( $h$ )	Raster of slope orientation values from DEM $h$
<b>Set and graph functions</b>	
HONEYCOMB( $x, s_{hex}$ )	Creates a honeycomb grid corresponding to polygon $x$ of $x$ with hexagonal elements having surface $s_{hex}$
PARTGRAPH( $G, n, W_{part}$ )	Partitions a graph $G$ into $n$ parts having weights $W_{part}$

---

#### Algorithm 1: GREECE main algorithm

---

```

1 begin
2   /* Compute candidate parcels specified spatially as polygons */
3    $P \leftarrow \text{MASK}(B_{layer}, R_{layers}, B_{uffers})$ 
4   for  $p \in P$ :
5     if SURFACE( $p$ )  $\geq s_{max}$ :
6        $P.\text{DELETE}(p)$ 
7        $P.\text{INSERT}(\text{PARTITION}(p, s_{max}, f_d))$  /* see algorithm 2 */
8   for  $p \in P$ :
9     if SURFACE( $p$ )  $< s_{min} \vee \text{DISTANCE}(p, i \in D_{layer}) > dt_i, dt_i \in \text{DistT}$ :
10       $P.\text{DELETE}(p)$ 
11  /* Compute, store de-spatialized features for each polygon p
12  (Section 3.2) */
13  for  $p \in P$ :
14     $p.\text{APPEND}(\text{DISTANCE}(p, N \in \text{NET}_{layers}))$ 
15     $p.\text{APPEND}(\text{SHAPE}(p), p.\text{APPEND}(\text{SURFACE}(p)))$ 
16     $p.\text{APPEND}(s_k \in \text{SURFACE}(p \cap \text{INTERSECTS}(p, LU_{layer},$ 
17     $\text{RTREEIDX}(LU_{layer})))$ 
18    /* Aggregate raster cell values, terrain features, within p */
19     $p.\text{APPEND}(\mu_n \in \text{ZONALSTAT}(\{h, \text{SLOPE}(h), \text{ASPECT}(h)\}, p, \mu))$ 
20     $p.\text{APPEND}(\sigma_n \in \text{ZONALSTAT}(\{h, \text{SLOPE}(h), \text{ASPECT}(h)\}, p, \sigma))$ 
21    /* Mean energy resource values per raster time series */
22     $p.\text{APPEND}(\{\mu_1, \mu_2, \dots, \mu_t\} \in \text{ZONALSTAT}(R_{maps}, p, \mu))$ 

```

---

### 3.1 Spatial placement and partitioning of polygons

*Slicing the base layer: extracting parcel polygons* The slicing of the whole study area is divided into two main steps. The first consists in identifying and removing

the restricted areas that intersect a base polygon (our study area) as well as zones beyond the distance threshold from given elements (electrical grid, road network, etc.). The procedure  $\text{MASK}(B_{\text{layer}}, R_{\text{layers}}, B_{\text{buffers}})$  applies set-based topological operators, that mask out portions of restricted layers and buffered zones, intersecting the base layer (Alg.1:line 3). It corresponds to a 2-dimensional difference operation. The result of this first step is a finite set  $P$  of new polygons, representing available land for potential power facilities, illustrated in Fig 2 (a).

The second step (Alg.1:lines 4-10), consists in filtering in a deterministic manner the polygons belonging to this set, based on their surface and distance to the grid. First we identify the parcels whose surface is beyond the allowed threshold. We developed a 2D space partitioning approach based on a k-way graph partitioning method, that partitions these parcels into smaller ones of suitable sizes (Algorithm 1: line7). Then, we prune further the resulting set of potential parcels according to the minimal surface threshold and distance to the grid, illustrated in Fig 2 (b). This last step is best handled using GIS geographical metric operators (Alg.1: lines 8-10). The extracted and computed parcels can all contribute to a solution, without inconsistent pruning of viable parcels from the standpoint of the threshold and land restriction constraints. Fig.2 illustrates the spatial layers masking process as well as the pruning of parcels below a surface threshold, and beyond a distance threshold to network layers (grid, roads, ...).

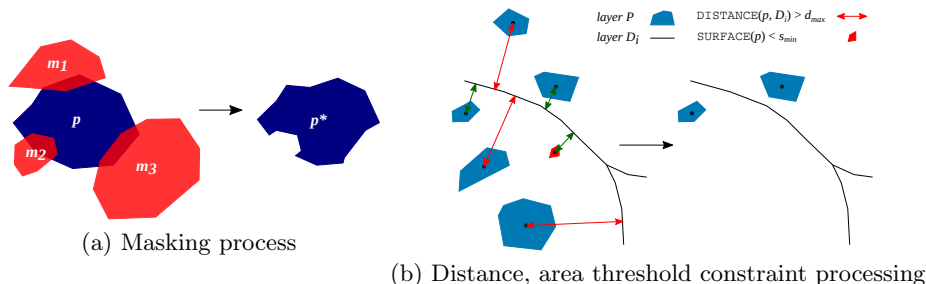


Fig. 2: Pruning restricted areas and threshold layers

*Spatial partitioning method* To partition a polygon into smaller plots of equal size, we propose a k-way graph partitioning approach, depicted in Alg. 2. First, we specify the initial polygon as a honeycomb mesh, that is a set of connected hexagonal plots of given size (line 6). We then map the mesh to a graph, and apply a k-way graph partitioning (lines 7, 20-29). Each hexagon denotes a vertex connected to its concomitant neighbors by unweighted and undirected edges. The  $k$  value is first initialized using a desaggregation factor, that sets the size of each hexagon (lines 3-5). The bigger the factor value, the smaller each hexagon and thus the more refined is the mesh. Each vertex is weighted with the corresponding hexagon surface. The weight of the sought clusters (final plots) is initialized (lines 8-13), to feed the k-way graph partitioning (line 15). The procedure derives  $k$  clusters of vertices, to reach the surface threshold of each plot. The algorithm minimizes the number of edge cuts and forces contiguous partitions [29], so that



**Algorithm 2:** Surface partitioning

---

```

1 def PARTITION( $p, s_{max}, f_d$ ): /* Partition polygon  $p$  into a set of
  polygons  $P$  of equal surface */
  Input : polygon  $p$ , maximal area per partition  $s_{max}$ , disaggregation
        factor  $f_d$ 
  Output : a set  $P$  of polygons
2 /* Initialization */
3  $k \leftarrow \lfloor \frac{SURFACE(p)}{s_{max}} \rfloor$  /* Number of targeted plots */
4 if  $k \leq 1$  and  $SURFACE(p) - s_{part} < s_{part}/f_d$ :
5   return  $\{p\}$ 
6  $H \leftarrow HONEYCOMB(p, area:s_{max}/f_d)$  /* create the mesh of hexagons */
7  $G \leftarrow TOGRAPH(H, SURFACE(hexa \in H))$ 
8 for  $i \in \{1, \dots, k\}$ :
9   /* Set the weight for each sought plot */
10   $W_{plot}.APPEND(s_{max})$ 
11 if  $SURFACE(p) \bmod s_{max} \neq 0$ :
12    $W_{plot}.APPEND(SURFACE(p) - n \cdot s_{max})$ 
13    $k \leftarrow k + 1$ 
14 /* k-way graph partitioning of  $G$  into a set of  $k$  clusters  $C$  */
15  $C \leftarrow PARTGRAPH(G, k, W_{plot})$ 
16 /* Convert the clusters of vertices into a set polygons */
17 for  $set \in C$ :
18    $P.INSERT(UNION(p_i \mid i \in set))$ 
19 return  $P$ 
20 def TOGRAPH( $H, W_{hexa}$ ): /* Convert the weighted mesh into a graph */
  Input : set of hexagons  $H$ , set of corresponding weights  $W_{hexa}$ 
  Output : a graph  $G$ 
21 /* Initialization */
22  $G \leftarrow GRAPH()$ 
23 for  $(h, w) \in (H, W_{hexa})$ :
24   /* set of polygons concomitant to  $h$ , frontiers */
25    $F \leftarrow INTERSECTS(h, H, RTREEIDX(H))$ 
26   for  $f \in F$ :
27      $G.INSERT(EDGE(h, f))$ 
28    $G.INSERT(NODE(p, weight:w))$ 
29 return  $G$ 

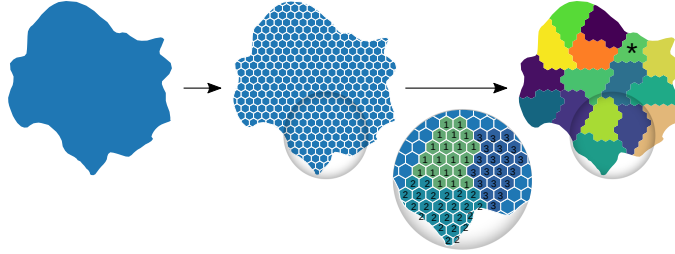
```

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the final aggregates present round-like geometries. The algorithm was developed using Python library `networkx` and the METIS package [30]. Finally the  $k$ -clusters are translated into  $k$  polygons (lines 17-18).

*Example 1.* The figure illustrate a 16-way graph partitioning of a 781 km<sup>2</sup> polygon into plots of 50 km<sup>2</sup>, using an hexagonal honeycomb mesh.  $k$  is initialized to  $\lfloor \frac{781}{50} \rfloor$ . The algorithm derives 15 plots between 49 km<sup>2</sup> and 51 km<sup>2</sup> plus one (marked with an asterisk) which fills the leftover space ( $\approx 32$  km<sup>2</sup>). The output

is a finite set of polygons of acceptable surface (below the maximum threshold).



### 3.2 Contextual data and resource time series de-spatialization

Geospatial data is an invaluable source of contextual information, to characterize in general, multiple land features and resources, but also their proximity with all sorts of infrastructure networks. The challenge when dealing with optimization problems evolving around resources, costs and constraints, is to seek a computational approach to specify and solve a problem as closely as possible to its real setting. A contribution of the proposed GIS-RO framework is to achieve this by using the qualitative and large spatio-temporal and contextual information analyzed and extracted through GREECE, with a de-spatialization process. The goal is to convert the polygons into items without their geo-referencing, and to associate to each the features relevant to the optimization module. Regarding energy planning, the features must capture many land properties, and resource time series, but also dimensions and distances that will allow a reliable conversion to technical costs for each candidate parcel.

The localization and maximal surface of a candidate parcel can provide numerous relevant information from the intersected data layers: 1) the distance to specific infrastructures such as substations, electrical grid or road network contributes to assessing energy losses as well as accessibility costs, 2) the maximal surface is linked to construction and maintenance costs [42,6,3]. In addition, terrain slope is a critical criterion for establishing power facilities [4,46]; in the same way, final cost might also be affected by land type and land use, or even the shape of the parcel. In the case of solar and wind energies, geo-referenced resource maps are available from satellite images or field studies [20,5,6]. By overlaying the previously sliced polygons with these raster images, it is therefore possible to aggregate the resource within each parcel. Essentially, the de-spatialization consists in translating the geography of each candidate into either static or dynamic quantifiable features. These features can then be integrated into energy models, converted into construction and operation costs, or used as constraints or in the objective functions of the optimization model. In the case of solar PV, GREECE extracts the following parameters from each candidate parcel: area, shape, distance to the grid, land use share, elevation, slope, aspect and solar GHI time series (Alg. 1:lines 13-20). The whole implementation has made use of the python libraries referred earlier. `SURFACE( $p$ )` provides information on the maximum power plant capacity that could eventually be set up within the parcel. `SHAPE` ranges from 0 to 1 and measures the roundness of a parcel, that is

how spread out a solar PV plant might eventually be. `DISTANCE` to the grid is computed from the polygon centroid and is used to get both connection costs and transmission losses. *Land use share* can be correlated to construction costs, as well as *elevation* (from DEM  $h$ ) using `SLOPE` and `ASPECT`. They may also be used as exclusion thresholds. Land use share is retrieved by computing the intersecting area between the given parcel and each attribute of a land use layer  $LU_{layer}$  (line 15). Elevation, slope and aspect are retrieved from the 3 arc second SRTM-based digital elevation model (DEM) [27] and by calculating average and standard deviation from raster cells overlapping with each candidate parcel (lines 17-18). Finally, *solar GHI time series* are obtained in the same way as with the DEM but for as many time steps as available solar radiation maps (line 20). As a result, each candidate parcel is now a compound item with geometric and terrain features, and time series of solar GHI values. In the case of solar PV, we have also converted GHI into power by adapting the `pvlb` library from the Sandia National Laboratory (SNL) [25].

#### 4 Optimization module - fractional knapsack approach

The Optimal planning and sizing of PV plants (OPSPV) is an optimization problem permeated with uncertainty, rooted in projection estimates from current data relative to the growth of energy demand and the resource values. As shown in Fig. 1, it takes the candidate parcels with their de-spatialized features to select the ones and their optimal size such that the PV power penetration in the network is maximized at minimal cost. We propose a robust optimization approach based on the seminal works of [8,14], that specifies uncertainty using deterministic intervals. They denote the robust bounds within which the uncertain data is known to take its value. This modelling approach enables reliable best and worst case planning scenarios to guide the decision makers, and to assess the impact of his risk adversity impact on the output scenarios. The specification of the problem is given in Fig. 3.

##### Robust constraint optimization model

The OPSPV, energy strategy planning problem can be modelled as a fractional knapsack problem with additional constraints. In this analogy, the knapsack corresponds to the forecast energy demand to be provided by existing and new intermittent RE sources (in  $KW/hr$ ), and the items are the candidate parcels with their potential supply ( $KW/hr$ ) plus their associated technical costs (installation relative to the size thus production ( $€/KW$ ), and connection to the grid and substation ( $€$ )). The objective is to maximize hourly penetration of additional RE power in the network while minimizing global costs.

We first specify the problem and then describe the model developed in terms of variables, constraints and cost functions.

*Variables* We consider two sets of variables that need to be linked to each other. Boolean variables relate to the selection or not of a candidate parcel, needed to determine whether the unit connection cost is applied or not ( $Ccon_i$ ). The area variables, ranging over a real interval, are involved in the energy production

**Given:**

Unit: Hour (per year)	$t \in H = \{1, \dots, 8760\}$
Unit: Candidate parcel	$i \in N = \{1, \dots, n\}$
Current hourly production from intermittent energy sources (KWh)	$Eint_t$
Current hourly production from non-intermittent energy sources (KWh)	$Ep_t$
Estimated global hourly power demand (KWh)	$Dem_t = [\underline{Dem}_t, \overline{Dem}_t]$
Nominal power of a PV unit (to convert plant size into power)	$Pnom$
Minimum and maximum area for each candidate parcel ( $m^2$ )	$Smin, Smax_i$
Estimated hourly production per PV unit ( $Wh/m^2$ )	$Ppv_{t,i} = [\underline{Ppv}_{t,i}, \overline{Ppv}_{t,i}]$
Minimal distance from the grid to centroid of a candidate PV parcel (m)	$Dg_i$
Transmission line unit cost (€/m)	$Clan$
Substation unit power cost (€/KW)	$Csta$

**Find:**

- The set of parcels where power stations will be built
- The surface to consider for each candidate parcel that is selected

**Cost functions:**

Sum of all costs of PV plant installation	$C = \sum_i (Ccap_i + Cop_i + Ccon_i + Csta_i)$
Unit capital cost for installing a PV power plant (€)	$Ccap_i$
Annual operational cost per new PV plant (€)	$Cop_i$
Unit connection costs for each new PV plant, transmission lines (€)	$Ccon_i$
Capital cost for new substation (€)	$Csta_i$
Total added PV energy production	$\sum_t PV_t$

**Such that the following constraints hold:**

- PV newly added production plus existing production are below the hourly demand
- PV existing and new production are less than 35% of the total energy demand per hour
- PV parcel size cannot exceed a maximal set size

Fig. 3: OPSPV problem specification

constraint and the installation, capital and operational costs, that depend on the size of a new PV plant.

$$\begin{aligned} \forall i \in N, \mathbf{B}_i &\in \{0, 1\} && 1 \text{ if parcel is selected, 0 otherwise} \\ \forall i \in N, \mathbf{SA}_i &\in [0.00..Smax_i] && \text{Area of a parcel} \end{aligned}$$

*Knapsack constraints* The first set of constraints relates to the forecast energy demand, using existing resources augmented with new PV production. It seeks to determine the capacity of new PV plants to contribute to the anticipated demand. Two scenarios are considered: 1) best case scenario (highest PV energy forecast and lowest forecast demand) and 2) worst case scenario (lowest PV energy forecast and highest forecast demand). This allows to study the impact of the decision maker risk adversity in planning the creation of new PV plants.

$$\text{Best case scenario: } \forall t \in H, \quad \sum_i \mathbf{SA}_i \times \overline{Ppv}_{t,i} + Eint_t + Ep_t \leq \underline{Dem}_t$$

$$\text{Worst case scenario: } \forall t \in H, \quad \sum_i \mathbf{SA}_i \times \underline{Ppv}_{t,i} + Eint_t + Ep_t \leq \overline{Dem}_t$$

*Network penetration constraints* The second set of constraints states that the amount of intermittent energy resource into the network should be less than 35 % of the total forecast energy demand per hour (upper bound) [17]. The time stamp is the hour. It is also set for the best and worst case scenarios:

Best case scenario:  $\forall t \in H, \Sigma_i \mathbf{SA}_i \times \overline{Ppv_{t,i}} + Eint_t \leq 0.35 \times \overline{Dem_t}$

Worst case scenario:  $\forall t \in H, \Sigma_i \mathbf{SA}_i \times \underline{Ppv_{t,i}} + Eint_t \leq 0.35 \times \overline{Dem_t}$

*Connecting parcel selection and size* The third set of constraints establishes a link between the Boolean and PV plant area variables. This relationship is needed to connect the energy production and the various costs. If a plant size is not null then the parcel is selected, and conversely if a parcel is not selected its size is forced to be null.

$$\forall i \in N, \mathbf{SA}_i \leq Smax_i \times \mathbf{B}_i, \mathbf{B}_i \times Smin \leq \mathbf{SA}_i$$

*Objectives and cost functions* The OPSPV problem has two main objective functions: 1) to maximize the total hourly RE energy production over the year through new PV energy production, 2) to minimize the total technical costs. Since the functions are in different units, a single weighted function is not meaningful, instead we seek the pareto frontier, by optimizing PV production function while constraining the cost function with more restrictive values at each run.

*Maximize PV production:* depending on the scenario considered,  $Ppv_{t,i}$  will take its highest estimate ( $\overline{Ppv_{t,i}}$  for best case) or lowest estimate ( $\underline{Ppv_{t,i}}$  for the worst case). The cost function to maximize is:

$$\Sigma_i \Sigma_t \mathbf{SA}_i \times Ppv_{t,i}$$

*Minimize costs: Modelling non-linear functions* Four cost functions are involved and relate to the installation and size of a PV plant as defined in Fig. 3. Typically, capital and operational costs are approximated as linear functions [9,24,19]. However, this approach is unrealistic as both the  $Cap_i$  and  $Cop_i$  costs are in fact non-linear, since they depend on the size of the plant (linked to the related number of PV panels) [31]. Basically the fewer the number of panels the highest the relative cost per panel. To get closer to reality, we thus consider an innovative approach using a piece-wise linear function such that  $a_i$  is the coefficient of the slope, and  $y_i$  the value of the coordinate where the new slope begins. It is illustrated below for  $Cap_i$ , and  $Cop_i$  follows a similar specification with different constants. Values have been set from [31]:

$$Cap_i = \begin{cases} a_1 \times Pnom \times \mathbf{SA}_i + y_1 & \text{if } 0_{MW} \leq \mathbf{SA}_i \times Pnom \leq 1_{MW} \\ a_2 \times Pnom \times \mathbf{SA}_i + y_2 & \text{if } 1_{MW} \leq \mathbf{SA}_i \times Pnom \leq 10_{MW} \\ a_3 \times Pnom \times \mathbf{SA}_i + y_3 & \text{if } 10_{MW} \leq \mathbf{SA}_i \times Pnom \end{cases}$$

On the other hand, the unit connection cost of a PV plant, and the capital cost of a new station for a plant, are both linear functions that depend respectively on the creation of the plant in a parcel with its Euclidian distance to the grid, and the unit cost of a substation proportional to the computed size of the plant. We have the following functions:

$$Ccon_i = Clan \times Dg_i \times \mathbf{B}_i, \quad Csta_i = Csta \times Pnom \times \mathbf{SA}_i$$

## 5 Experimental study and evaluation

The proposed GIS-RO framework seeks to make powerful use of multi-scale contextual information for spatial decision making and optimization. It is evaluated on the timely challenge in the region of French Guiana, where the objective is to reach the energy policy plan of 100% renewable by the year 2030, first by increasing PV, then biomass. The challenge lies in the strategic planning of solar PV scenarios using contextual real data characterized by spatio-temporal patterns and permeated with uncertainty (resource projections). In this section we present our results and analysis. Input data layers, retrieved from various national and world databases [33,32,28,26], and associated buffer values are depicted in Table 1. In addition, maximum distance to both power grid and road network has been set to 20 km, twice the value commonly used [6,39]. Land surface area minimum and maximum thresholds for establishing solar PV plants are respectively set to 1.5 ha [44] and 50 ha [17]. Finally, regarding plot resource, monthly solar GHI time series derived from satellite-based raster images [5,20] have been disaggregated at the hour using an updated version of a synthetic generation model [1,2,38].

Table 1: Land management scenario used in this study for restricted areas.

Layer	Protected areas	Forest areas	Urban areas	Flood savanna	Water bodies	Shore	Power grid	Road network	Wetland	Dune/Sand	Rice/Orchard
<b>Buffer (m)</b>	500	200	200	100	100	100	100	30	0	0	0
<b>Refs</b>	[45]	[6]	[45,3]	[41]	[40,41]	[40]	[39,3,41]	[39,3,41]	[41]		

The GREECE module was implemented in Python using GIS-Python libraries recalled in the paper. It provides de-spatialized data items to the OPSPV module, which was implemented using IBM ILOG OPL CPLEX Optimization studio, on a 2 processors (Intel(R) Xeon(R) CPU E5-2609 v4 @1.70GHz) of 32 Go RAM. The GREECE module led to the extraction of 133 candidate parcels with their relevant features. The execution CPU time for the GREECE module is about 460 s. (reading files: 30 s; mask: 380 s.; partitioning: 3 s.; feature + monthly resource extraction: 50 s.), handled as a one off spatial placement pre-processing. The optimization CPU time varies from 23 s to 47 s depending on the bound set on the constrained objective function (runtime differences come from handling piece-wise linear functions that depend on the park sizes).

*Data sets* Restricted area layers handled in MASK correspond to a total of 21088 geographical objects. Here, the base layer  $B_{layer}$  corresponds to Guiana’s land use  $LU_{layer}$ , which gathers 2643 polygons. Road network and power grid used in distance threshold computation are made of 2247 lines. Monthly solar resource is represented by a raster set of  $12 \times 3999 \times 3999$  cells. Global energy demand and existing production data are known from the sources and extractions from records of 2016 [18]. For the 2030 horizon we projected hourly energy demand values according to EDF estimations of worst case 5% annual growth and best case of 2% annual growth.

## Results and analysis

We analyzed three aspects of relevance to the decision maker and network manager (power plant energy investors in Guiana and EDF) that are made possible with the combination of geographical and temporal contextual information and optimization: 1) the impact of the spatio-temporal energy patterns on the geographic selection process (Fig. 4 and 6 (b)), 2) the study of the risk adversity comparing best and worst case scenarios (Fig. 5), 3) the identification of robust planning investment scenarios where the optimal plants show to be identical regardless of the degree of spatio-temporal uncertainty on the power resource (Fig. 6 (a)).

Fig. 4 depicts the resulting spatial variation of the solar GHI patterns (derived by GREECE) on the produced power from the optimal solar PV plants (location and size) whose placement is visible in Fig. 6 (b). P1 and P4 sites (P2 and P3) have similar patterns for they are located in the same solar potential cluster zone. Essentially, it shows how our GIS-RO approach manages real site spatial arrangement so that the global output power is robust through time from the optimal PV plants: impact of their RE intermittency on future network power management is limited.

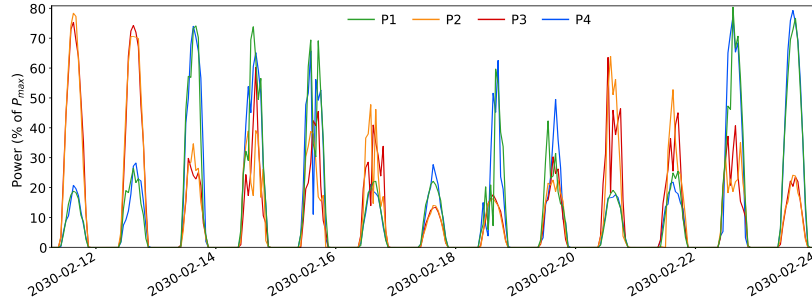


Fig. 4: Normalized output power from solar PV sites of Fig. 6.

Fig. 5 gives information about (a) the volume of solar PV plants one may install within the region without threatening the power grid in the long-term, and (b) its corresponding final share in the energy mix. As long as both Pareto lines remain together in Fig. 5 (a), the solution is robust, i.e. power generation over time from selected plants fills up *the same free energy volume* regardless of the scenario: corresponding PV sites can be explored safely in the limits of their maximum capacity estimated by the RO. In contrast, once the best case reaches its plateau, and so Pareto lines split in half (around 40 M€), power generation no longer fills up the same volume. At this point, the more the energy generated in the worst case scenario, the more it exceeds the energy generation limit in the best case: the risk grows as much as the gap between both lines.

Finally, Fig. 6 evaluates the robustness of the investment according to spatio-temporal uncertainty on the resource: i) estimated GHI, energy potential (in blue), ii) its mitigation by a random uniform noise per hour and per parcel, between 0 and 10% (in green) and iii) between 0 and 20% (in red) respectively.

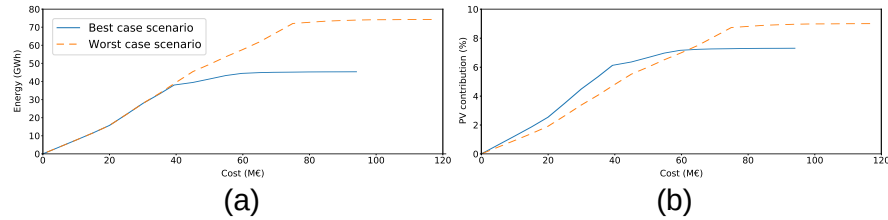


Fig. 5: Pareto charts for both scenarios with respect to (a) generated energy and (b) PV penetration.

The safety zone lies below a cost of 70 M€ (C70), meaning that the selected PV sites are the same for all resource time series projections. Those sites are sorted by ascending parcel size area from the smallest (P1) to the largest (P4). The investment costs grow naturally when the optimal PV plant size grows within its corresponding parcel area (fractional knapsack optimization).

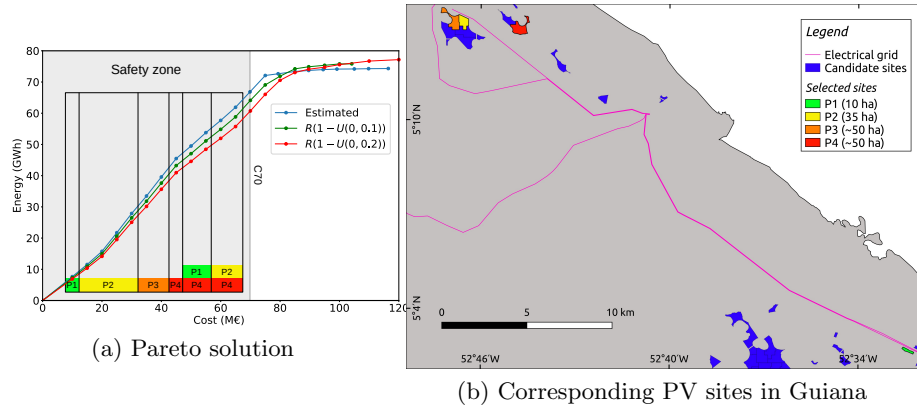


Fig. 6: Robustness of the worst-case scenario solution with decreasing resource

## 6 Conclusion

In this paper we have proposed a two-step specification and novel computational approach of the spatio-temporal placement and energy planning problem. We addressed key challenges of sustainable science in terms of spatial decision making and usage of complex contextual data, constraints and time series of resources. The presented GIS-RO framework allows for real world and large scale applications to be solved through an integrated approach at the interface of GIS science, graph and robust optimization models and methods. The case study showed in particular the importance of taking into account actual resource patterns and allowing for fractional parcel selection to optimize power plants location and size, and thus optimize the power penetration at minimal cost. Current work includes its generalization to include the cost-effectiveness of energy storage considered not profitable to this date in Guiana, and the generalization to biomass resources that raises a complex temporal renewability issue of the resource.



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