Unified Picture of Anionic Redox in Li/Na-ion Batteries

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Anionic redox in Li-rich and Na-rich Transition Metal Oxides (Arich-TMOs) has emerged as a new paradigm to increase the energy density of rechargeable batteries. Ever since, numerous electrodes delivering anionic extra-capacity beyond the theoretical cationic capacity were reported. Unfortunately, most often the anionic capacity achieved in charge is partly irreversible in discharge. A unified picture of anionic redox in Arich-TMOs is here designed to identify the electronic origin of this irreversibility and to propose new directions to improve the cycling performance of the electrodes. The electron localization function (ELF) is introduced as a holistic tool to unambiguously locate the oxygen lone-pairs in the structure and follow their participation in the redox activity of Arich-TMOs. The charge-transfer gap of transition metal oxides is proposed as the pertinent observable to quantify the amount of extra-capacity achievable in charge and its reversibility in discharge, irrespectively of the material chemical composition. From this generalized approach, we conclude that the reversibility of the anionic capacity is limited to a critical number of O-hole per oxygen, $h^O \leq 1/3$.

GENERAL CONTEXT

Increasing the energy density of cathode materials is a central goal of ongoing research in Li/Na-ion batteries. This implies improving simultaneously the material potential and capacity. Whereas potential can be easily tuned through an appropriate choice of the redox centre of the electrochemical reaction, [1, 2] capacity is more challenging to increase without penalizing the material structure. Thanks to the cumulative cationic and anionic activity recorded in Li/Na-rich transition metal oxides (Arich-TMOs), [3–9] anionic redox emerged as a new paradigm to increase energy density. However, extra-capacities due to anions generally lead to structural instabilities resulting in significant irreversibility in the first cycle, [10] capacity and potential fading upon cycling, [11] cationic migrations [12, 13] and oxygen loss. [6, 12, 14–16] This yields continuous decomposition of the electrode upon cycling which constitutes a major drawback for practical applications. The opportunity to play with M/M' chemical substitutions [7], structural dimensionality [9] or cation-disorder [17] has raised hopes that a winning combination can suppress these irreversibilities, hence enabling long-term cycling for high-energy-density electrodes. Recent examples supporting this line were reported by different groups and summarized in several reviews. [18–20] Among them, the tri-dimensional β -Li₂IrO₃ model electrode [9] combines improved cycling performance and a record capacity of 2.5 Li/Ir; the lighter Li_{1.3}Nb_{0.3}Mn_{0.4}O₂ electrode [7] displays the highest first-charge capacity (> 300 mAh/g) ever reported and the Na_{2/3}[Mn_{0.72}Mg_{0.28}]O₂

electrode [21, 22] shows reversible anionic redox without Na-excess, cationic disorder or O₂ release. [22] Over the past 5 years experimental and theoretical studies have contributed to figure out the origin of anionic redox as arising from oxygen lone-pair states in the material electronic structure. [16, 20, 23–25] However, debates and controversial interpretations persist in the literature on the reversibility of the anionic process upon charge/discharge. Yet, these questions are paramount to decide whether the objective of high-energy-density batteries can be achieved with Arich-TMOs materials.

This paper proposes a unified picture of anionic redox in Arich-TMOs, irrespectively of their structural-type and electronic structure. Based on rigorous concepts of electronic (band) structure theory, we investigate the impact of the material electronic ground state, A-excess, M/M' chemical substitution and cationic order/disorder on the electrochemical activity of the O-network. This conceptual approach is validated by first-principles calculations through the computation of the Electron Localization Function (ELF). [57] ELF is a topological tool of the electron density that probes the regions of space where paired-electrons are confined, and is used, for the first time in Arich-TMOs, to demonstrate the participation of oxygen lone-pairs in the redox activity of these electrodes. Within this framework, we identify the charge-transfer gap of TMOs (Δ_{CT}) and the number of O-holes per oxygen (h^O) as pertinent descriptors to quantify the anionic capacity achievable in charge and its reversibility in discharge. This provides experimentalists with measurable quantities to infer the overall electrochemical performance of their materials, and new rational recipes to exit the maze of anionic redox.

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FIG. 2. **Electron Localization Function** computed from first-principles DFT+U calculations (isovalues of 0.7) for $\text{Li}[\text{Li}_{1/3}\text{M}_{2/3}]\text{O}_2$ ($\text{M} = \text{Mn}, \text{Ru}, \text{Sn}$) showing an equivalent number of oxygen lone-pairs per oxygen (one $|\text{O}_{2s}$ and one $|\text{O}_{2p}$), irrespectively of the M-O bond covalency. For $\text{Na}_{2/3}[\text{Mg}_{1/3}\text{Mn}_{2/3}]\text{O}_2$, the apparent Mn/Mg substitution in fact corresponds to a Na/Mg substitution (Mg^{2+} acting as 2Na^+ in the charge compensation) so that the material stoichiometry is $x = 1/3$ (" A_2MO_3 "). For $\text{Na}_{4/7}[\square_{1/7}\text{Mn}_{6/7}]\text{O}_2$, one and two oxygen lone-pairs per oxygen occur in the Mn-rich (orange) and Mn-poor (red) O-environments, respectively.

When the two states get close in energy, the electronic ground-state of the material is (quasi)degenerate which is unstable towards any structural distortion that removes the degeneracy. The distortion must lower the crystal symmetry to allow efficient interactions between $(\text{M-O})^*$ and $|\text{O}_{2p}$, both states having different symmetries in the undistorted structure. It corresponds to the formation of a three-centered M-(O-O) species, through a so-called Reductive Coupling Mechanism (RCM) [4, 24] which opens a gap in the material electronic structure. Interestingly, the transition metal initially oxidized is being reduced when the structural reorganization takes place, due to a redistribution of the $|\text{O}_{2p}$ electrons into the new M-(O-O) bonding states (highlighted in orange in Fig. 3). The participation of the anions in the electrochemical activity of Arich-TMOs is then activated through the dynamic of the cationic process (O to M charge transfer). As a proof of concept, we computed the ELF isovalue for a typical Mott-Hubbard system, namely the $\beta\text{-Li}_{2-z}\text{IrO}_3$ model electrode. [9] As shown in Fig. 3, one $|\text{O}_{2p}$ per oxygen is lost in the delithiated structure, concomitantly with the appearance of weak O-O bonds (see Supplementary Information S2 for details).

Charge Transfer Systems

Charge-transfer systems are described by an empty

FIG. 3. **Dynamics of A-removal in Mott-Hubbard Systems.** Qualitative electronic structure of Arich-TMOs displaying a Mott-Hubbard electronic ground state (left). The electrostatic stabilization (resp. destabilization) of the $(\text{M-O})^*$ antibonding states (resp. $|\text{O}_{2p}$ states) upon e^- (resp. Li^+) removal is shown by the dashed lines. The reductive coupling mechanism (grey inset) lifts the electronic degeneracy into M-(O-O) bonding and antibonding bands represented in orange, which induces a $|\text{O}_{2p}$ to $(\text{M-O})^*$ charge transfer. In discharge, the re-insertion of Li should involve the $(\text{M-O})^*$ states hence allowing the system the return back to the undistorted structure through a perfectly reversible mechanism. Note that if all M(d) states are not involved in the RCM, a fraction of M(d)-states (dotted blue band) may remain in the RCM-gap, therefore leading to some irreversibility in discharge. The participation of the $|\text{O}_{2p}$ states in the oxidation process is illustrated for the $\beta\text{-Li}_{2-z}\text{IrO}_3$ electrode which was recently reported as exhibiting a mixed cationic-anionic redox activity. The ELF value computed for the lithiated ($z = 0$) and delithiated ($z = 2$) phases clearly shows the loss of one oxygen lone-pair per oxygen upon oxidation.

metallic band lying above the fully-filled anionic band (here the $|\text{O}_{2p}$ band) and separated in energy by the charge-transfer gap Δ_{CT} (see Fig. 4). The removal of electrons from the $|\text{O}_{2p}$ localized states generates unstable oxygens that must recombine to recover a stable electronic configuration (octet rule). As a result of O-O pairing, the narrow $|\text{O}_{2p}$ band splits into σ , π , π^* and σ^* discrete bands with an amplitude as large as the O-O distance is short, i.e. as the $(\text{O-O})^{n-}$ species are oxidized (red and yellow triangles in Fig. 4). As a robust criteria, a given $(\text{O-O})^{n-}$ dimer is stable as long as its highest occupied states lie below the lowest unoccupied metallic band. Accordingly, the amplitude of Δ_{CT} with respect to $\text{O}^{2-}/(\text{O}_2)^{2-}$, $\text{O}^{2-}/(\text{O}_2)^{-}$ or O^{2-}/O_2 redox energies is the pertinent descriptor to predict the amount of extra-capacity achievable in charge and its reversibility in discharge.

Following the horizontal blue line of Fig. 4, $(\text{O-O})^{n-}$ species are stable as long as $\Delta_{CT} > \Delta_{O-O}^{\sigma}$ (before (1)). As for the reductive coupling mechanism discussed above,

the anionic oxidation is fully reversible in discharge, since the electronic states involved in oxidation and reduction are similar. From (1) to (2) the metallic band lies between the π^* and σ^* bands, so that $(\text{O}_2)^{2-}$ peroxides can form. As a result of the $\sigma^*/\text{M}(d)$ band inversion, a cationic reduction is expected in the first-step discharge, leading to voltage hysteresis. The peroxide reduction in a second-step discharge obviously depends on the capacity used for the cationic process. Above (2) the metallic band lies below the π^* -states of the oxidized species ($\Delta_{\text{O-O}}^\pi > \Delta_{\text{CT}}$). This results in the release of O_2 gas concomitantly with a cationic reduction, through a mechanism known as a reductive elimination. [35]

Remarkably, the weak occurrence of transition metal peroxides reported in the literature [36, 37] suggests that most TMOs display Δ_{CT} band gaps lower than the $\text{O}^{2-}/(\text{O}_2)^{2-}$ redox energy (below (1)). In contrast, alkali or alkali-earth oxides display much larger Δ_{CT} and are known to form peroxides. This strongly suggests that $(\text{O}_2)^{2-}$ peroxides in charged Arich-TMOs should only occur in $\text{M}(d)$ -free/ $\text{A}(s,p)$ -rich O-environments, as exemplified in the $\text{Ba}_5\text{Ru}_2\text{O}_{11}$ peroxide/oxide phase. [38] In this structure, the σ^* states of peroxides ($d_{\text{O-O}} = 1.5 \text{ \AA}$) are raised in energy far above the metallic band, thus preventing their reduction in discharge.

III. The Unified Picture of Anionic Redox

All mechanisms described above can be put together to build a unified picture of anionic redox in Arich-TMOs. In this general framework, the number of holes per oxygen, h^{O} , is shown to be the critical parameter governing the reversibility of the anionic process.

In the most general case of Arich-TMOs combining cationic disorder and chemical substitutions, the oxygen network consists in a statistical distribution of various O-sublattices, each of them having a different number of $|\text{O}_{2p}|$ lone-pairs due to different $\text{A}/\text{M}/\text{M}'$ local environments. $|\text{O}_{2p}|$ states being non-bonding, their energy is primarily dictated by the electrostatic field exerted by the surrounding cationic charges. The lower the cationic charge around one oxygen, the smaller its Madelung potential and the higher in energy its $|\text{O}_{2p}|$ states in the electronic structure. How many holes are generated upon charge on each O-sublattice thus depends (i) on the relative energy of the electrochemically active O-sublattices, i.e. how homogeneous is the O-network, and (ii) on the material electronic ground-state, i.e. how much of the total theoretical capacity is available for the anionic process. Knowing this, the overall electrochemical behavior of Arich-TMOs can be deduced from the superimposition of each O-sublattice individual activity, accounting for their statistical weight in the pristine material, and following the mechanisms described above. This approach is illustrated in Fig. 5 for a representative set of $\text{A}[\text{A}_x\text{M}_{1-x}]\text{O}_2$ showing different $\text{A}/\text{M}/\text{M}'$ compositions and distributions and a theoretical capacity corresponding to $(1+x)$ electrons. The important message of this

FIG. 4. **Dynamics of the oxidation process in charge-transfer Arich-TMOs.** Qualitative electronic structure of Arich-TMOs displaying a charge transfer electronic ground-state in the reduced phase (left). The splitting of the $|\text{O}_{2p}|$ narrow band into discrete σ , π , π^* and σ^* states is highlighted by the red ($\Delta_{\text{O-O}}^\sigma$) and yellow ($\Delta_{\text{O-O}}^\pi$) triangles, as a function of the decreasing O-O distance (bottom horizontal axis) and the increasing oxidation state of the $(\text{O-O})^{n-}$ species (top horizontal axis). The different domains of anionic activity are represented by the intervals delimited by (1) and (2). The (1) to (2) narrow domain highlights the weak ability of transition metals to stabilize true peroxides in their structure (Δ_{CT} generally smaller than the $\text{O}^{2-}/(\text{O}_2)^{2-}$ redox energy), in contrast to $\text{A}(s,p)$ metals showing much larger Δ_{CT} gaps in the oxide phases.

figure is that $h^{\text{O}} \leq x$ is required for the anionic process to be reversible. Above this critical value, the anionic oxidation in charge is partially irreversible in discharge, except for O-sublattices having $\text{M}(d)$ -free/ A -rich local environments for which a reversible $\text{O}^{2-}/(\text{O}_2)^{2-}$ redox pair can exist.

For homogeneous O-networks, $h^{\text{O}} \leq x$ implies that at least $1 - x$ electron of the total capacity is consumed by a preceding cationic process involving one or more electro-active metals (Fig. 5a). The voltage profile of these materials should display nicely reversible electrochemical processes (see Fig. 6a) and a potential drop between the cationic and anionic reactions, as the signature of two distinct $\text{M}^{n+}/\text{M}^{(n+1)+}$ and $\text{O}^{2-}/(\text{O-O})^{2(2-x)-}$ redox pairs. The anionic process should be associated with a larger polarization than the cationic process, due to the structural reorganization of the O-network. [39] This electrochemical behavior is exemplified by the tridimensional $\beta\text{-Li}_2\text{IrO}_3$ electrode [9] showing well-defined reversible plateaus upon charge/discharge, no voltage hysteresis and limited irreversible capacity. 3D structures should be favored over 2D structures in which cationic migration is triggered by the interlayer electrostatic in-

FIG. 5. Unified picture of anionic redox in Arich-TMOs. Cationic and anionic processes expected for $A[A_xM_{1-x}]O_2$ ($0 < x \leq 1/3$) showing different A/A'/M/M' compositions and distributions. The cationic and anionic processes are represented by blue and red rectangles, respectively, the area of which being correlated to reversible (dashed) and irreversible (plain) capacities. Mott-Hubbard and charge-transfer regimes are distinguished by a negative and positive Δ_{CT} , respectively. M' refers to an electrochemically inactive metal having no impact on the number of $|O_{2p}|$ lone-pairs in the structure (pink M' = strongly correlated TM with half-filled d -band, post-transitional metal or d^0 metal). A' refers to an electrochemically inactive metal/vacancy increasing the number of $|O_{2p}|$ lone-pairs in the structure (green A' = A(s, p) mono- or divalent metal or metal vacancy). The number of oxygen lone-pairs per oxygen is indicated in yellow and h^O is calculated for each system by subtracting the cationic capacity to the total capacity. For disordered materials, the statistical weight of each O-sublattices is represented by the c_i coefficients. The total theoretical capacity is equivalent for all examples ($1 + x$ electrons) except for the last example in which the $A[A_xM_{1-x}]O_2$ general formulation is no longer valid due to the A/A' substitution.

stability at low A-content. This phenomenon was shown to limit the reversible capacity of the layered α - Li_2IrO_3 electrode [8] compared to its 3D β -polymorph. [9] Favoring electronic delocalization in 2D structures through the increase of bond covalency or with temperature should contribute against this instability. This is supported by the series of TM-chalcogenides (MX_2 or MX_3 , X=S, Se, Te) [40, 41] showing stable layered structures and by the layered Li_2RuO_3 electrode showing full reversible capacity when cycled at $50^\circ C$. [42]

Any M/M' chemical substitution for an electrochemically inactive M' metal invariably leads to partial irreversibility of the anionic process due to the increase of h^O above the critical x value (Fig. 5b). Above x , the highly oxidized O-network should disproportionate into h^O -related fractions of O^{2-} , $(O_2)^{2-}$ and O_2 sublattices with relative weights set by the chemical composition

FIG. 6. Schematic galvanostatic curves of A-Rich TMOs. Illustration of the cationic (blue) and anionic (red) processes in A-rich TMOs for the different scenarios given in Figs. 3 and 4. (a) Fully reversible cationic and anionic process with no O_2 release and no cation migration in charge. (b)-(c)-(d) The first part of the discharge corresponds to a cationic activity (blue) due to O_2 release at high-charging. This leads to a hysteresis between charge/discharge (yellow). When O_2 gas release occurs in first charge due to cationic migration/disorder, the process is not reversible leading to a persistent hysteresis in further cycles and a S-shape curve due to the multiplication of TM and (O-O) redox centers (b). The plateaus in charge are recovered if no O_2 release occurs at high charging and if cationic migrations are fully reversible in discharge (c). The capacity loss in charge due to O_2 gas release (red rectangle) is partially compensated in discharge (blue rectangle) by the activation of a novel TM redox couple (d).

of the pristine structure. Cationic migrations should take place from the critical $h^O = x$ state-of-charge to assist the disproportionation. Oxygens having more cationic vacancies in their local environment will be primarily oxidized, and prone to O_2 gas release through the partial reduction of the surrounding transition metal. An hysteresis is expected in the voltage profile of the electrode and the total capacity achieved in charge cannot be fully recovered in discharge (see Fig. 6b). Most Arich-TMOs reported in the literature belong to this category. They correspond to the general formulation $A[A_x(M_{1-y}M'_y)_{1-x}]O_2$ with $M' = d^0$, half-filled d -band TM with large U splitting (e.g. Mn^{4+} , Fe^{3+}), or post-transitional (e.g. Sn^{4+} , Te^{6+}) metal. These electrodes display large voltage hysteresis, cationic migration and a capacity loss linearly correlated to y , as exemplified by the series of $Li_2[Ru_{1-y}M'_y]O_2$ ($M' = Sn$, Ti , Mn) [4, 5, 43] and $Li_2[Ir_{1-y}Sn_y]O_2$. [8] Note that, in rare cases, the TM reduction induced by O_2 release may activate a cationic redox-pair in discharge that was not accessible in first charge. This could allow recovering, at least partially, the first-charge capacity in further cycles (see Fig. 6c). Reaching the complete substitution

of M for an inactive M' metal leads to charge-transfer materials, such as Li_2MnO_3 , [10, 44] in which the theoretical capacity is fully supported by the anions, i.e. $h^O = (1+x)/2$. Unless x is decreased to activate a cationic redox-pair, [45, 46] charge-transfer TMOs should display poor electrochemical performance [10] associated with a progressive decomposition of the electrode upon cycling, persistent voltage hysteresis and capacity fade in the voltage profile (see Fig. 6d). Finally, chemical A/A' substitutions with A' being highly reducing metals (large Δ_{CT}) appears as the only way to achieve a reversible anionic capacity with $h^O > x$ (see Fig. 5e) due to the possible stabilization of peroxides ($h^O = 1$) in M(d)-free/A'-rich environments. However, the statistical weight of this O-sublattice must be significant to benefit to the anionic capacity, which implies large A/A' substitution ratio y , i.e. low capacity and poor electronic conductivity.

Noteworthy, any release of O_2 gas in charge lowers h^O in further cycles. Consequently, Arich-TMOs can display nicely reversible electrochemical cycles after a first charge that kills the activity of the most unstable O-sublattices. This is exemplified for instance by the $\text{Li}_{1.2}[\text{Mn}_{0.54}\text{Co}_{0.13}\text{Ni}_{0.13}]\text{O}_2$ [3] and $\text{A}_{1.3}\text{Nb}_{0.3}\text{Mn}_{0.4}\text{O}_2$ (A = Li, Na) electrodes [47, 48] sustaining reversible capacity of ~ 250 and ~ 300 mAh/g, respectively. Interestingly, the lithiated $\text{Li}_{1.3}\text{Nb}_{0.3}\text{Fe}_{0.4}\text{O}_2$ electrode shows significantly lower performance compared to its Mn-based homologue. While this behavior was attributed by the authors to a Fe-O bond covalency larger than Mn-O, [48] our unified picture shows it arises from different h^O . Alike Li_2MnO_3 , $\text{Li}_{1.3}\text{Nb}_{0.3}\text{Fe}_{0.4}\text{O}_2$ is a charge-transfer insulator (inactive Fe^{3+} ions confirmed by DFT calculations in ref. [48]) for which the total theoretical capacity is fully supported by the anions ($h^O = (1+x)/2$). In the Mn-based system, 0.4 electrons are consumed by a preceding $\text{Mn}^{3+}/\text{Mn}^{4+}$ cationic process, leading to significantly lower h^O and better cycling performance, after the first cycle. The same comparison can be made between the Li_2MnO_3 [10] and the Mn-defective $\text{Na}_{4/7}[\square_{1/7}\text{Mn}_{6/7}]\text{O}_2$ electrodes. [28] While the former displays no cationic redox and highly irreversible anionic redox, the latter shows nicely reversible cationic and anionic redox processes, very similar to the $\beta\text{-Li}_2\text{IrO}_3$ electrode [9] thanks to a limited extra-capacity ($h^O < x$). Finally, approaching the limits of cationic and anionic electrochemical activity with the Li-rich layered rocksalt Li_3IrO_4 ($x = 1/2$) electrode shows that the delithiated IrO_4 electrode converts into IrO_3 at the end of charge, which limits h^O to 1/3 in further cycles. [25] Overall, these examples

highlight the negligible role of M-O bond covalency in the electrochemical behavior of Arich-TMOs and suggest that $h^O = 1/3$ is the upper limit for achieving reversible anionic capacity in $\text{A}[\text{A}_x\text{M}_{1-x}]\text{O}_2$ electrodes. Obviously, any chemical substitution lowering h^O through the activation of a cationic redox-pair, is a good strategy to favor structural stability and more reversible anionic electro-activity, as nicely exemplified by transition metal oxyfluorides. [27, 49]

CONCLUSION

So far, most Arich-TMOs reported in the literature as displaying high-energy-density due to anionic redox, are prone to structural instabilities that prevent their use in practical applications. Several alternatives have been proposed to limit or suppress these irreversibilities, among which the increase of M-O bond covalency, the chemical substitution of M for d^0 metals or the use of cation-disordered rocksalt structures. The unified picture developed in this paper contrasts with these statements in showing that the number of holes per oxygen (h^O) is the critical parameter to sustain a reversible anionic capacity. From a representative set of materials reported in the literature, $h^O = 1/3$ appears as the critical value to avoid O_2 release and achieve fully reversible anionic redox. Measurable quantities such as the TMO band gap (Δ_{CT}) and the x stoichiometry are therefore sufficient to determine h^O and to infer the electrochemical behavior of $\text{A}[\text{A}_x\text{M}_{1-x}]\text{O}_2$ electrodes.

Within this general framework, the best candidates for high-energy-density are those cumulating an optimal cationic capacity and an anionic capacity limited to $h^O \leq 1/3$. Tri-dimensional structures should be preferred over layered structures to prevent structural instability at low A-content and take advantage of the full theoretical capacity. Ordered structures should favor homogeneous O-networks should avoid h Very few TMOs should satisfy these requirements, in particular when they also have to meet industrial specifications such as cost, toxicity and natural abundance. Overall, strategies devoted to the activation of anionic redox as a lever to improve the energy density of electrode materials are risky as they implicitly means that anions become less electronegative than cations at some point, therefore questioning the structural stability of the materials. The triptych of high-potential, high-capacity and high structural stability still appears out of our current reach and calls for trade-offs.

[1] Padhi, A. K., Nanjundaswamy, K. S., Masquelier, C., Okada, S. & Goodenough, J. B. Effect of structure on

the $\text{Fe}^{3+}\text{-Fe}^{2+}$ redox couple in iron phosphates. *J. Electrochem. Soc.* **144**, 1609-1613 (1997).

- [2] Saubanère, M., Ben Yahia, M., Lebègue, S. & Doublet, M.-L., *Nat. Commun.* **5** 5559 (2014).
- [3] Koga, H., Croguennec, L., Ménétrier, M., Dohil, K., Belin, S., Bourgeois, L., Suard, E., Weil, F. & Delmas, C., Reversible oxygen participation to the redox processes revealed for $\text{Li}_{1.20}\text{Mn}_{0.54}\text{Co}_{0.13}\text{Ni}_{0.13}\text{O}_2$. *J. Electrochem. Soc.* **160** A786-A792 (2013).
- [4] Sathiya, M. *et al.* Reversible anionic redox chemistry in high-capacity layered-oxide electrodes. *Nat. Mater.* **12** 827-835 (2013).
- [5] Sathiya, M., Ramesha, K., Rousse, G., Foix, D., Gonbeau, D., Prakash, A. S., Doublet, M.-L. & Tarascon, J.-M., High performance $\text{Li}_2\text{Ru}_{1-y}\text{Mn}_y\text{O}_3$ cathode materials for rechargeable lithium-ion batteries: their understanding. *Chem. Mater.* **25** 1121-1131 (2013).
- [6] Luo, K. *et al.* Charge-compensation in 3d-transition-metal-oxide intercalation cathodes through the generation of localized electron holes on oxygen. *Nat. Chem.* **8** 684-691 (2016).
- [7] Yabuuchi, N. *et al.* High-capacity electrode materials for rechargeable lithium batteries: Li_3NbO_4 -based system with cation-disordered rocksalt structure. *Proc. Nat. Acad. Sci.* **112**(25), 7650-7655 (2015).
- [8] McCalla, E. *et al.* Visualization of O-O peroxo-like dimers in high-capacity layered oxides for Li-ion batteries. *Science* **350**, 1516-1521 (2015).
- [9] Pearce, P.E. *et al.* Evidence for anionic redox activity in a tridimensional-ordered Li-rich positive electrode β - Li_2IrO_3 . *Nat. Mater.* **16** 580-587 (2017).
- [10] Robertson, A. D. & Bruce, P. G., Mechanism of Electrochemical Activity in Li_2MnO_3 . *Chem. Mater.* **15**, 1984-1987 (2003).
- [11] Ito, D., Liu, Y., Chong, S. & Wu, Y.-F., Cyclic deterioration and its improvement for Li-rich layered cathode material $\text{Li}[\text{Ni}_{0.17}\text{Li}_{0.2}\text{Co}_{0.07}\text{Mn}_{0.56}\text{O}_2]$. *J. Power Sources* **195**, 567-573 (2010).
- [12] Croy, J. R., Iddir, H., Gallagher, K., Johnson, C. S., Benedek, R., Balasubramanian, M., First-charge instabilities of layered-layered lithium-ion-battery materials. *Phys. Chem. Chem. Phys.* **17**, 24382 (2015).
- [13] Gent, W. E. *et al.* Coupling between oxygen redox and cation migration explains unusual electrochemistry in lithium-rich layered oxides. *Nat. Commun.* **8**, 2091-1-12 (2017).
- [14] Lee, E. & Persson, K. A., Structural and Chemical Evolution of the Layered Li-Excess Li_xMnO_3 as a Function of Li Content from First-Principles Calculations. *Adv. Energy Mater.* **4**, 1400498 (2014).
- [15] Qian, D., Xu, B., Chic, M. & Meng, Y. S., Uncovering the roles of oxygen vacancies in cation migration in lithium excess layered oxides. *Phys. Chem. Chem. Phys.* **16** 14665-14668 (2014).
- [16] Xie, Y., Saubanère, M., Doublet, M.-L., Requirements for reversible extra-capacity in Li-rich layered oxides for Li-ion batteries. *Energy Environ. Sci.* **10**, 266-274 (2017).
- [17] Urban, A., Matts, I., Abdellahi, A. & Ceder, G., Computation Design and Preparation of Cation-Disordered Oxides for High-Energy-Density Li-Ion Batteries. *Adv. Ener. Mater.* 1600488-1-8 (2016).
- [18] Li, B. & Xia, D., Anionic Redox in Rechargeable Lithium Batteries. *Adv. Mater.* **29** 1701054-1-28 (2017).
- [19] Li, W., Song, B. & Manthiram, A., High-voltage positive electrode materials for lithium-ion batteries. *Chem. Soc. Rev.* **46**, 3006-3059 (2017).
- [20] Assat, G. & Tarascon, J.-M., Fundamental understanding and practical challenges of anionic redox activity in Li-ion batteries. *Nature Energy* **3** 376-286 (2018).
- [21] Yabuuchi, N., Hara, R., Kubota, K., Paulsen, J., Kumakura, S., Komaba, S., A new electrode material for rechargeable sodium batteries: P2-type $\text{Na}_{2/3}[\text{Mg}_{0.28}\text{Mn}_{0.72}\text{O}_2]$ with anomalously high reversible capacity. *J. Mater. Chem. A* **2**, 16851-16855 (2014).
- [22] Maitra, U. *et al.* Oxygen redox chemistry without excess alkali-metal ions in $\text{Na}_{2/3}[\text{Mg}_{0.28}\text{Mn}_{0.72}\text{O}_2]$. *Nature Chemistry* **10** 288-295 (2018).
- [23] Seo, D.-H., J., Urban, A., Malik, R., Kang, S. Y. & Ceder, G., The structural and chemical origin of the oxygen redox activity in layered and cation-disordered Li-excess cathode materials. *Nature Chemistry* **8**, 692-697 (2016).
- [24] Saubanère, M., McCalla, E., Tarascon, J.-M. & Doublet, M.-L., The intriguing question of anionic redox in high-energy density cathodes for Li-ion batteries. *Energy Environ. Sci.* **9**, 984-991 (2016).
- [25] Perez, A. J., Jacquet, Q., Batuk, D., Iadecola, A., Saubanère, M., Rousse, G., Larcher, D., Vezin, H., Doublet, M.-L. & Tarascon, J.-M., Approaching the limits of cationic and anionic electrochemical activity with the Li-rich layered rocksalt Li_3IrO_4 . *Nat. Energy* **2**, 954-962 (2017).
- [26] Becke, A. D. & Edgecombe, K. E., A simple measure of electron localization in atomic and molecular systems. *J. Chem. Phys.* **92** 5397-5403 (1990).
- [27] House, R., Jin, L., Maitra, U., Tsuruta, K., Somerville, J., Forstermann, D., Massel, F., Duda, L., Roberts, M. R. & Bruce, P. G., Lithium manganese oxyfluoride as a new cathode material exhibiting oxygen redox. *Energy & Environ. Sci.* **11** 926-932 (2018).
- [28] Mortemard de Boisse, B., Nishimura, S.-I., Watanabe, E., Lander, L., Tsuchimoto, A., Kikkawa, J., Kobayashi, E., Asakura, D., Okubo, M. & Yamada, A., Highly Reversible Oxygen-Redox Chemistry at 4.1 V in $\text{Na}_{4/7-x}[\text{X}_{1/7}\text{Mn}_{6/7}\text{O}_2]$ (X: Mn Vacancy). *Adv. Energy Mater.* **2018** 1800409 1-7.
- [29] Hong, J., Xiao, D.-D., Zhang, X.-D., Yin, Y.-X., Guo, Y.-G., Gu, L. & Wan L.-J., Review — Lithium-excess layered cathodes for lithium rechargeable batteries. *J. Electrochem. Soc.* **162**, A2447-A2467 (2015).
- [30] Rozier, P. & Tarascon, J. M., Review — Li-rich layered oxide cathodes for next-generation Li-ion batteries: chances and challenges. *J. Electrochem. Soc.* **162**, A2490-A2499 (2015).
- [31] Croy, J. R., Balasubramanian, M., Gallagher, K. G. & Burrell, A. K. Review of the U. S. Department of Energy's 'Deep Dive' effort to understand voltage fade in Li- and Mn-rich cathodes. *Acc. Chem. Res.* **48**, 2813-2821 (2015).
- [32] Zheng, J., Myeong, S., Cho, W., Yan, P., Xiao, J., Wang, C., Cho, J. & Zhang, J.-G., Li- and Mn-rich cathode materials: challenges to commercialization. *Adv. Energy Mater.* **7**, 1601284 (2016).
- [33] Hy, S., L. H., Zhang, M., Qian, D., Hwang, B.-J. & Meng, Y. S., Performance and design considerations for lithium excess layered oxide positive electrode materials for lithium ion batteries. *Energy Environ. Sci.* **9**, 1931-1954 (2016).
- [34] Zaanen, J., Sawatzky, G. A. & Allen, J. W. Band gaps and electronic structure of transition-metal compounds. *Phys. Rev. Lett.* **55**, 418-421 (1985).

- [35] Crabtree, R. H., The Organometallic Chemistry of the Transition Metals. Third Edition. (John-Wiley & Sons, Inc., New-York, 2001).
- [36] Toriumi, K. & Saito, Y. Electron-Density Distribution in Crystals of α -K₂CrO₄. *Acta Cryst. B* **34** 3149-3156 (1978).
- [37] Fischer, J., Veillard, A. & Weiss, R. *Theoretica Chimica Acta* **24** 317-333 (1972).
- [38] Grimaud, A. *et al.* Chemical Activity of the Peroxide/Oxide Redox Couple: Case Study of Ba₅Ru₂O₁₁ in Aqueous and Organic Solvents. *Chem. Mater.* **30** 3882-3893 (2018).
- [39] Assat, G., Foix, D., Delacourt, C., Iadecola, A., Dedryvère, R. & Tarascon, J.-M., Fundamental interplay between anionic/cationic redox governing the kinetics and thermodynamics of lithium-rich cathodes. *Nat. Commun.* **8** 2219 (2017).
- [40] Rouxel, J., Anion-cation redox competition and the formation of new compounds in highly covalent systems. *Chem. Eur. J.* **2** 1053-1059 (1996).
- [41] Rouxel, J., Some solid state chemistry with holes: anion-cation redox competition in solids. *Curr. Sci.* **73** 31-39 (1997).
- [42] Yabuuchi, N., Material Design Concept of Lithium-Excess Materials with Rocksalt-related Structures for Rechargeable Non-Aqueous Batteries. *The Chem. Record* **18**, 1-19 (2018).
- [43] Sathiyar, M. *et al.* Origin of voltage decay in high-capacity layered oxide electrodes. *Nat. Mater.* **14** 230-238 (2015).
- [44] Kalyani, P., Chitra, S., Mohan, T. & Gopukumar, S., Lithium metal rechargeable cells using Li₂MnO₃ as the positive electrode. *J. Power Sources*, **80**, 103-106 (1999).
- [45] Armstrong, A. R., Robertson, A. D., Bruce, P. G., Overcharging manganese oxides: Extracting lithium beyond Mn⁴⁺. *J. Power Sources* **146**, 275-280 (2005).
- [46] Freire, M., Lebedev, O.I., Maignan, A., Jordi, C & Pralong V., Nanostructured Li₂MnO₃: a disordered rock salt type structure for high energy density Li ion batteries. *J. Mater. Chem. A* **5** 21898-21902 (2017).
- [47] Sato., K., Nakayama, M., Glushenkov, A. M., Mukai, T., Hashimoto, Y., Yananka, K., Yishimura, M., Ohta, T. & Yabuuchi, N., Na-Excess Cation-Disordered Rocksalt Oxide: Na_{1.3}Nb_{0.3}Mn_{0.4}O₂. *Chem. Mater.* **29** 5043-5047 (2017).
- [48] Yabuuchi, N. *et al.* Origin of stabilization and destabilization in solid-state redox reaction of oxide ions for lithium-ion batteries. *Nat. Commun.* **7**:13814 (2016).
- [49] Lee, J. *et al.* Reversible Mn²⁺/Mn⁴⁺ double redox in lithium-excess cathode materials. *Nature* **556** 185-190 (2018).

Methods

Spin-polarized calculations were performed using the VASP code [50, 51] within the density functional theory (DFT) framework. Perdew-Burke-Ernzerhof (PBE) functional [52] with a generalized gradient approximation form (GGA-PBE) was adopted to treat the exchange correlation energy. The rotationally invariant Dudarev method (DFT+U) [53] was applied to account

for strongly correlated *d* electrons with different U_{eff} values. The range-separated hybrid functional [54] (HSE06) was also used for a sake of comparison with DFT+U. To obtain a good numerical sampling of the electron densities in Brillouin zone, the Monkhorst-Pack technique [55] was used. Moreover, with the application of the projector augmented wave (PAW) technique, [56] the plane-wave energy cutoff was determined to be 600 eV. For structural relaxations, all atomic coordinates and lattice parameters were fully relaxed until the force acting on each atom is less than 3.10^{-3} eV.Å⁻¹.

ELF: A pertinent tool to characterize and visualize $|O$ lone-pairs in a material is known as the Electron Localization Function (ELF). To the best of our knowledge, this tool has never been used in A-rich TMOs, although $|O$ lone-pairs are central in the rationalization of their electrochemical properties. It is a topological tool of the electron density that pinpoints the regions of space where paired electrons are confined. Initially designed by Becke and Edgecombe for atoms and molecules, [57] it was developed in the Density Functional Theory framework by Savin [58] and is becoming popular in material science due to its holistic approach to electronic structures. [59] ELF measures the Pauli repulsion through the probability of finding an electron of spin σ in the vicinity of another electron of same spin. The explicit formulation is:

$$ELF = \left[1 + \left\{ \frac{K(\mathbf{r})}{K_h[\rho(\mathbf{r})]} \right\}^2 \right]^{-1} \quad (1)$$

where K is the curvature of the electron-pair density $\gamma_2(r_1^q, r_2^q)$, $\rho(\mathbf{r})$ the electron density and K_h the value of K for the homogeneous electron gas with density ρ . The ELF values were computed for the different materials given as examples in the paper, at various Li/Na-contents. ELF values range from 0 (no paired electrons) to 1 (paired electrons) and are here plotted for 0.7 iso-values in Fig. 1, Fig. 2 and Supplementary Information Fig.S1, Fig.S2.

Data Availability

The datasets generated during and/or analysed during the current study are available from the corresponding author on reasonable request.

References

- [50] Kresse, G. & Furthmüller, J., Efficiency of ab-initio total energy calculations for metals and semiconductors using a plane-wave basis set. *Computational Materials Science* **6** 15-50 (1996).
- [51] Kresse, G. & Hafner, J., Ab initio molecular dynamics for liquid metals. *Phys. Rev. B* **47** 558-561 (1993).

- [52] Perdew, J. P., Burke K. & Ernzerhof, M., Generalized Gradient Approximation Made Simple. *Phys. Rev. Lett.* **77** 3865-3868 (1996).
- [53] Dudarev, S. L., Botton, G. A., Savrasov, S. Y., Humphreys, C. J. & Sutton, A. P., Electron-energy-loss spectra and the structural stability of nickel oxide: An LSDA+U study. *Phys. Rev. B* **57** 1505-1509 (1998).
- [54] Heyd, J., Scuseria, G. E. & Ernzerhof, M., Hybrid functionals based on a screened Coulomb potential. *J. Chem. Phys.* **118** 8207-8210 (2003).
- [55] Monkhorst, H. J. & Pack, J. D., Special points for Brillouin-zone integrations. *Phys. Rev. B* **13** 5188-5192 (1976).
- [56] Blöchl, P. E., Projector augmented-wave method. *Phys. Rev. B* **50** 17953-17979 (1994).
- [57] Becke, A. D. & Edgecombe, K. E. A simple measure of electron localization in atomic and molecular systems. *J. Chem. Phys.* **92** 5397-5403 (1990).
- [58] Savin, A., Jepsen, O., Flad, J., Andersen, O. K., Preuss, H. & von Schnering, H. G., Electron Localization in Solid-state Structures of the Elements: the Diamond Structure. *Angew. Chem. Int. Ed. Engl.* **31** 187-188 (1992).
- [59] Causà, M.; D'Amore, M.; Gentile, F.; Menendez, F.; Calatayud, M. Electron Localization Function and Maximum Probability Domains analysis of semi-ionic oxides crystals, surfaces and surface defects. *Computational and Theoretical Chemistry* **1053**, 315-321 (2015).

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Author Contributions

All authors contributed equally to the DFT calculations & analyses. MS and MLD developed the theoretical framework and wrote the paper.

Additional Information

Supplementary information is available in the online version of the paper. Reprints and permissions information is available online at www.nature.com/reprints. Correspondence and requests for materials should be addressed to M.-L.D or M.S.

Competing financial interests

The authors declare no competing financial interests.