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QUANTIFYING VARIATION IN SPECIATION AND EXTINCTION RATES WITH CLADE DATA

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High-level phylogenies are very common in evolutionary analyses, though they are of-1 ten treated as incomplete data. Here we provide statistical tools to analyze what we 2 name 'clade data', that are the ages of clades together with their numbers of species. 3 We develop a general approach for the statistical modeling of variation in speciation 4 and extinction rates, including temporal variation, unknown variation, and linear and 5 nonlinear modeling. We show how this approach can be generalized to a wide range of 6 situations, including testing the effects of life-history traits and environmental variables 7 on diversification rates. We report the results of an extensive simulation study to assess 8 the performance of some statistical tests presented here as well as of the estimators of 9 speciation and extinction rates. These latter results suggest the possibility to estimate 10 correctly extinction rate in the absence of fossils. An example with data on fish is 11 presented. 12

KEY WORDS: birth-death models, extinction, maximum likelihood, speciation, stem
 ages.

The study of the tempo and mode of evolution has experienced a new wave 15 of interest from evolutionists using new mathematical and statistical tools 16 to analyze molecular phylogenies (Sanderson and Donoghue 1996; Ricklefs 17 2007). Following some initial breakthrough (e.g., Nee et al. 1992, 1994), sig-18 nificant progress has been achieved in biologically relevant statistical mod-19 eling of diversification, such as quantifying temporal variation in diversifi-20 cation (Paradis 2011; Hallinan 2012) or assessing the effects of biological 21 traits on speciation and extinction rates (Maddison et al. 2007; FitzJohn 22 et al. 2009; FitzJohn 2010). Recent advances have also been accomplished 23 in integrating molecular and fossil data (e.g., Morlon et al. 2011; Didier et al. 24 2012). 25

Most of these recent statistical developments have focused on analyz-26 ing complete phylogenies. Incomplete phylogenies are often treated as a 27 separate case in order to take missing data into account (Pybus et al. 2002; 28 FitzJohn et al. 2009; Stadler 2011). The most common form of such data is 29 a phylogeny resolved at a high level accompanied by the number of species 30 associated to each tip of the tree. On the other hand, the ages of clades 31 together with the numbers of species (named here 'clade data') have been 32 a neglected source of data in the analysis of diversification. Magallón and 33 Sanderson (2001) provided some methods for the analysis of such data and 34 applied them to angiosperms. They particularly developed various estima-35 tors of the (net) rate of diversification of a clade giving its age and number 36 of species. 37

The relative lack of interest towards clade data may come from the fact that, for a given clade, its complete phylogeny contains more information than the pair of values 'age + number of species'. However, for a collection of clades, such data are a valuable source of information for several reasons.

First, clades defined by higher-level taxa (e.g., families, orders) are clearly 42 43 identified for almost all groups of living beings and their numbers of species are in many cases already known. Second, phylogenetic relationships among 44 higher-level taxa have been much more studied than within them, so it is 45 more straightforward to date the age of a clade rather than the divergences 46 among its species. Third, the fossil record is generally more informative on 47 the origin of higher-level taxa compared to species or other low-level taxa. 48 Fourth, it is easier to examine the impact of the species concept on the 49 definition of clade data rather than on a phylogeny since, in the former the 50 species concept will mostly affect the number of species while in the latter it 51 will be often hard to infer different phylogenies under those distinct species 52 definitions. Clade data have also some disadvantages: the inherent lack 53 of temporal resolution within each clade makes it impossible to study the 54 variation in diversification within them. 55

In the present paper, we extend the approach presented by Magallón 56 and Sanderson (2001) and present statistical tools for the inference of di-57 versification patterns and processes with clade data. Our approach assumes 58 that each clade, instead of having its own speciation and extinction rates, 59 comes from a 'statistical population of clades' so that maximum likelihood 60 inference is straightforward. With this rationale, we show how to make 61 inference on variation in diversification parameters among clades using dif-62 ferent modeling tools, including testing the effects of life-history traits and 63 environmental variables and the case where variation is a priori unknown. 64 We also present the results of a simulation study in order to assess the sta-65 tistical performance of several tests and estimators presented in this paper, 66 and finally we apply our approach on a data set of fish. 67

68 Statistical Modeling Approach

Throughout this paper we assume that diversification proceeds with speci-69 ation (λ) and extinction (μ) rates which are the probabilities that a species 70 splits into two daughter-species or goes extinct during a very short time. 71 We denote as X_t the number of species in a clade of age t where this may 72 be either the stem age of the clade (divergence time of the clade from its 73 sister-clade) or its crown age (time to the most common recent ancestor 74 of the species belonging to the clade). Specifically, using equation 8 from 75 Kendall (1948), we can write the probability that X_t takes a specific integer 76 value x: 77

$$\Pr(X_t = x | \theta, X_0 = 1) = \eta_t (1 - \eta_t)^{x - 1} \qquad x \ge 1,$$
(1)

where θ is a vector of parameters specifying how speciation and extinction 78 rates vary through time and η_t is a function of these parameters. The 79 conditioning on $X_0 = 1$ emphasizes that in this paper we consider stem 80 groups. For the case of crown groups $(X_0 = 2)$, the probabilities must 81 be summed on all possible combinations. In most applications, stem groups 82 are considered because the origin of a group is inferred from its relationships 83 with its sister-group. On the other hand, deriving the crown age of a group 84 requires to estimate the age of the most recent common ancestor of its species 85 which is usually more complicated because it requires to sample all species 86 in the clade. On the other, inferring stem ages requires one species from the 87 clade and one from its sister-clade. 88

Various forms exist for these probabilities depending on the parameterization of θ and whether we wish to condition them on survival of the lineage until present or not. For instance, if extinction rate is zero and speciation rate is constant, then $\eta_t = e^{-\lambda t}$. This is the Yule (1924) model. Models with ⁹³ a non-null extinction rate are called birth–death models (Kendall 1948).

The point of conditioning on no extinction is important when analyzing data on actual groups because total extinction of these groups did not occur. Thus the probabilities must be modified accordingly, otherwise this would result in underestimated extinction rates (Rabosky et al. 2007).

Let us consider for the moment the simple Yule model. The expected 98 number of species at time t is given by $E(X_t) = e^{\lambda t}$. From this expectation, 99 a simple estimator of λ based on the method of moments is $\hat{\lambda} = \ln(x)/t$ 100 (Magallón and Sanderson 2001). When considering a single clade, and in 101 the absence of more detailed information, it does not seem possible to go 102 further in the inference. When considering more than one group (e.g., the 103 families within an order or a class), researchers usually estimate λ separately 104 for each group, then proceed with standard statistics (e.g., McPeek 2008). 105 This approach assumes that each clade is characterized by its own speciation 106 rate. On the other extreme, one may assume that speciation rate is the same 107 in all groups so that the observed data are independent outcomes of the 108 same diversification process. Thus, it is possible to use maximum likelihood 109 inference using equation 1. The likelihood function is: 110

$$\prod_{i} \Pr(x_i|\lambda),\tag{2}$$

where $Pr(x|\lambda)$ is a simplified notation of equation 1. We may expect less bias in the estimates from this approach, but also the possibility to test hypotheses based on fitting alternative models.

The assumption of equal speciation rates among clades is, certainly in most cases, unrealistic (Purvis et al. 1995; Paradis 2005; Alfaro et al. 2009). However, since we have several observations we may model the variation in this parameter with a statistical modeling approach. We explore several such approaches below. Firstly, we consider approaches based on deterministic variation between two or more groups of clades. Secondly, we consider how temporal variation in speciation and extinction rates can be modeled and assessed. Thirdly, we develop an approach handling unknown variation based on mixture modeling, including the combination of mixtures with a linear modeling of the speciation rate. Finally, we attack the problem of estimating extinction rates.

125 Variation Among Clades

A simple way to model variation in diversification among clades is to assume that there are two categories: some clades diversify with speciation rate λ_1 and the others with rate λ_2 . The data are made of n_1 and n_2 clades in each category, respectively. The likelihood function is:

$$\prod_{i_1=1}^{n_1} \Pr(x_{i_1}|\lambda_1) \prod_{i_2=1}^{n_2} \Pr(x_{i_2}|\lambda_2).$$

Note that each clade is assigned to a category a priori, although there is no assumption on whether λ_1 is greater, or smaller, than λ_2 . The null hypothesis $\lambda_1 = \lambda_2$ can be tested by fitting this model and the null model whose likelihood is given by equation 2: the likelihood-ratio test (LRT) comparing these two models follows a χ^2 distribution with df = 1. An alternative is to use the Akaike information criterion (Akaike 1973).

The present approach is easily generalized to more than two categories: let us denote the number of categories as K, then the likelihood function would become the product of K products:

$$\prod_{j=1}^{K} \prod_{i_j=1}^{n_j} \Pr(x_{i_j} | \lambda_j),$$

where n_j is the number of clades in the *j*th category. The LRT comparing this model with the null model of homogeneous diversification follows a χ^2 with df = K - 1.

These models assume, mostly for simplicity, that there is no extinction ($\mu = 0$); however, variation in extinction rate can be incorporated in a straightforward way. For instance a model with two categories diversifying with the same λ but with different extinction rates has the following likelihood function:

$$\prod_{i=1}^{n_1} \Pr(x_{i_1}|\lambda,\mu_1) \prod_{i=1}^{n_2} \Pr(x_{i_2}|\lambda,\mu_2),$$

which could be compared with the null model with $\mu > 0$ whose likelihood is:

$$\prod^{N} \Pr(x_i | \lambda, \mu),$$

with $N = n_1 + n_2$. This test is related, but not identical, to the tests of equal diversification using sister-clades where the ages of clades are not needed (Paradis 2012b).

The supplementary materials provide annotated R code explaining how to build and fit any model following the present approach.

154 Linear Modeling

Following the previous section, two extreme models can be defined: the simplest one where all clades diversify at the same rate, and the most complex one where each clade has its own parameter(s). This second model will be overparameterized for a likelihood approach. Nevertheless, it is possible to model variation in diversification parameters with linear models. For instance, we may know a priori some variables that are likely to affect the value of speciation rate (e.g., body size), and a model that relates such 'covariates' to speciation rate may be an appropriate candidate to model the variation in diversification among clades. We use here a standard strategy to model variation in a rate with respect to a covariate z:

$$g(\lambda_i) = \beta z_i + \alpha_i$$

where λ_i is the speciation rate in clade *i*, *g* is a function used to transform the 165 rate in order to linearize the relationship, and β and α are two parameters. 166 Here β controls the effect of z on λ : if $\beta > 0$ then species with large values 167 of z will speciate faster than those with small values of z (and inversely if 168 $\beta < 0$). It is possible to consider more than one predictor in which case 169 the number of parameters is equal to the number of predictors plus one. 170 Nonlinear models can also be considered. Each clade has its own speciation 171 rate given by (with g^{-1} being the inverse transformation of g): 172

$$\lambda_i = g^{-1}(\beta z_i + \alpha), \tag{3}$$

which is used to calculate the likelihood defined by equation 2: the likelihood function is then maximized to estimate β and α (see code in the Supplementary Material). A common choice for g is the logit function, $\ln(\lambda_i/(1-\lambda_i))$, so g^{-1} gives:

$$\lambda_i = \frac{1}{1 + \mathrm{e}^{-(z_i\beta + \alpha)}},$$

The null model is defined by fixing $\beta = 0$ in which case $\lambda = 1/(1 + e^{-\alpha})$ for all clades. The logit function is well suited for parameters varying between 0 and 1 which is the case for speciation rates considered on geological time
scales (million of years). However, speciation rates may be larger than one
on shorter scales. Other transformations can be used such as the one used
below.

It must be noted that the variation among clades as modeled in the previous section is a special case of linear models where the membership of a clade to a category is coded with a discrete variable and this variable is entered as a predictor into the linear model after coding it into binary 0/1 variable(s) (see appendix in Paradis 2005, for details). Therefore, continuous and categorical predictors can be combined in the linear model.

189 **Temporal Variation**

Kendall (1948) studied the birth-death model in a very general way, in-190 cluding the cases where λ and μ vary through time. Thus it is possible to 191 derive the probability density of the distribution of the x_i 's when diversifi-192 cation changed through time. The likelihood can be defined and fit in the 193 same way as above. Such a temporal model can be compared with the null 194 model of constant diversification with a χ^2 test whose df will be equal to 195 the number of additional parameters in the first model. As before, tempo-196 ral variation may reflect speciation and/or extinction rate(s). The simplest 197 temporal model has two rates before and after a given time point in the past, 198 so it has one additional parameter than the null model. Note that if the 199 time point is unknown, it could be estimated from the data so there would 200 be two additional parameters. However, a wide variety of temporal models 201 can be defined in ape (Paradis et al. 2004) using the function dbdTime where 202 the temporal variation is defined by the user with a standard R function. 203

204 Unknown Variation

The above models assume that diversification parameters vary in relation to some known variables, either categorical or continuous. On the other hand, it is possible that these variables are not observable. Such unknown variation can be modeled with two approaches depending on whether we assume that the diversification parameters vary in a discrete or continuous manner.

A mixture of distributions is based on the assumption that observations come from two or more categories each characterized by its own distribution, but the assignment of an observation to a particular category is unknown (see Flury et al. 1992, for a biological example). As a simple example, consider a mixture of two Yule processes, then the likelihood function will be:

$$\prod_{i=1}^{N} f \operatorname{Pr}(x_i|\lambda_1) + (1-f) \operatorname{Pr}(x_i|\lambda_2), \qquad (4)$$

where f is the proportion of clades in the first category. This model has 217 three parameters $(\lambda_1, \lambda_2 \text{ and } f)$ and can be compared with the null model 218 of homogeneous speciation with a LRT with df = 2. The idea is easily 219 generalized to more than two mixtures: a mixture with K Yule models 220 would have 2K-1 parameters. As above, the mixture may involve speciation 221 and/or extinction rate(s). By contrast to the situation above where clades 222 were assigned to categories a priori, there is here no assignment a priori. 223 On the other hand, assignment a posteriori is possible by calculating the 224 relative contributions to the likelihood function. 225

The idea may even be further generalized to include mixtures of linear models. Suppose we know that one variable, say body size, has a significant effect on speciation rate but there is some other, unknown, variation in this parameter that we want to model with a mixture. Then it is possible to calculate the λ_i 's with equation 3 and use them to compute the likelihood with eq. 4. Each category would have its own parameters β and α , so a model with K categories has 3K - 1 parameters.

The second approach assumes that, in the case of a Yule model, λ varies 233 continuously across clades following a specified distribution whose parame-234 ters are estimated from the data. A transformation of λ is useful so that it 235 follows a normal distribution: $g(\lambda) \sim \mathcal{N}(\mu_{\lambda}, \sigma_{\lambda}^2)$. A useful transformation 236 here is the complementary log-log transformation: $g(\lambda) = \ln(-\ln(\lambda))$. As 237 above we do not know the value of λ for a given clade, but this time instead 238 of a discrete sum we have to do a continuous integration. The likelihood 239 function is thus: 240

$$\prod_{i=1}^{N} \int_{-\infty}^{\infty} f_{\mathcal{N}}(u|\mu_{\lambda}, \sigma_{\lambda}^{2}) \Pr(x_{i}|g^{-1}(u)) \mathrm{d}u,$$

where $f_{\mathcal{N}}$ is the density function of the normal distribution. A graphical representation of the variation in λ is obtained with the inverse transformation $g^{-1}(u) = \exp(-e^u)$ with the dentity of u computed with the normal distribution and the estimates $\hat{\mu}_{\lambda}$ and $\hat{\sigma}_{\lambda}^2$.

245 Estimating Extinction Rates

The estimation of extinction rates in the absence of fossil data has appeared to be a complicated issue (Paradis 2004, 2011; McPeek 2008; Aldous et al. 2011; Morlon et al. 2011; Didier et al. 2012; Hallinan 2012). To try to tackle this problem, we implemented a procedure which fits a birth-death model estimating λ and μ simultaneously. These estimates are denoted as $\hat{\lambda}_{BD}$ and $\hat{\mu}_{BD}$.

252 Simulation Study

The present statistical modeling approach offers many possibilities and it 253 would take a large number of simulations to assess the statistical proper-254 ties of all of them. Instead, we focus on a few key questions. What is the 255 statistical power to detect a difference in diversification between two groups 256 of clades? How powerful is the test to detect temporal variation in diver-257 sification? What is the statistical power to detect unknown variation in 258 diversification between two groups of clades using mixtures? Finally, what 259 is the precision of the λ and μ estimators? 260

To address these four questions, we ran four sets of simulations. First, we 261 considered a simple two-category scenario with n_1 and n_2 clades simulated 262 with rates λ_1 and μ_1 and λ_2 and μ_2 , respectively. The times of evolution 263 were drawn from a uniform distribution: $t_i \sim \mathcal{U}(10, 20)$. A phylogeny was 264 simulated under a birth-death process during a time t_i using ape starting 265 from a single species. The number of species surviving at time t_i , x_i , was 266 extracted and the pairs (x_i, t_i) were analyzed as described above using a Yule 267 model. The LRT testing the null hypothesis of homogeneous diversification 268 was computed, and the rejection rate was assessed under different sets of 269 parameter values: $n_1 = n_2 = \{1, 3, 5, 10, 20\}, \lambda_1 = \{0.1, 0.15, 0.2\}, \lambda_2 = 0.1, \lambda_3 = 0.1$ 270 $\mu_1 = \{0, 0.05\}, \ \mu_2 = \{0, 0.05\}.$ 271

Second, we performed simulations under three scenarios with different values of diversification rates before and after 30 time units. We first generated 100 values of t from a uniform distribution between 10 and 50. We then simulated clades with constant, increasing, or decreasing diversification rate. The number of species was extracted as before, and two models were fitted: the null Yule model of constant diversification, and an alternative model assuming different speciation rates before and after 30 time units (as above $\mu = 0$ was assumed). The rejection rates of the LRTs comparing both models were computed.

Third, a scenario similar to the first one was considered: the difference 281 is that the simulated clades were not identified to a particular category so 282 the data were analyzed with a mixture of Yule models. We used K = 2, 283 $n_1 = n_2 = \{10, 20, 50\}$, and $t_i \sim \mathcal{U}(10, 20)$. Four combinations of speciation 284 and extinction rates were used: (i) the null hypothesis is true and there is 285 no extinction: $\lambda_1 = \lambda_2 = 0.1$, $\mu_1 = \mu_2 = 0$; (ii) the null hypothesis is false 286 and there is no extinction: $\lambda_1 = 0.1$, $\lambda_2 = 0.2$, $\mu_1 = \mu_2 = 0$; (iii) the null 287 hypothesis is false but only μ varies: $\lambda_1 = \lambda_2 = 0.2$, $\mu_1 = 0, \mu_2 = 0.1$; and 288 (iv) same than before with stronger variation in μ : $\lambda_1 = \lambda_2 = 0.2, \ \mu_1 = 0$, 289 $\mu_2 = 0.15.$ 290

Finally, we performed an assessment of the precision of the estimators of speciation and extinction rates using five combinations of λ and μ : (0.1, 0), (0.1, 0.03), (0.1, 0.06), (0.2, 0.1), and (0.2, 0.15). Here $t_i \sim \mathcal{U}(10, 30)$ and n = 100.

The simulations were replicated 1000 times. Annotated R (R Development Core Team 2012) code is available in the Supplementary Material with guidelines on how to run these simulations so that the readers can adapt them to their own problems. Besides, we did not attempt to compare our method with previous ones because some scenarios considered here cannot be analyzed by the latter (e.g., the third scenario does not seem to be tractable with Magallón and Sanderson's method).

302 Application to Fish Data

We used the data from Vega and Wiens (2012) who compiled the number of species, stem age, and percentage of marine fish species for 22 orders and

super-orders and for 97 families. They also provided a phylogeny for the 305 22 higher taxa which allowed to compare our estimates with those obtained 306 from the combined analysis of phylogeny and species richness data (Paradis 307 2003). All data were unmodified from the original publication and are avail-308 able at http://dx.doi.org/10.1098/rspb.2012.0075. With this data set, we 309 explored the variation in diversification using different mixtures of Yule and 310 birth–death models. We also tried to assess whether this variation is due to 311 differences in the speciation or in the extinction rates. 312

313 Results

314 Simulation Study

The first set of simulations showed that, overall, the LRT testing for dif-315 ferent diversification rates between two categories of clades had satisfactory 316 statistical properties (Table 1). The type I error rate (rejection rate when 317 the null hypothesis is true, i.e., $\lambda_1 = \lambda_2$ and $\mu_1 = \mu_2$) was, as expected, 318 close to 5% (first and seventh lines in Table 1). However, when $\lambda - \mu$ was 319 the same in both categories, the rejection rate was greater than 5% (eighth 320 line in Table 1) showing that the present test does not test for equal di-321 versification rate. In the cases where the null hypothesis was not true, the 322 rejection rate varied as expected: it was greater for larger sample sizes (n_1) 323 and for larger contrast in the speciation or extinction rate. Interestingly, if 324 one category of clades had smaller μ while λ was the same, then the test was 325 able to detect this difference; however, the statistical power was less than 326 when the same contrast in diversification was due to different λ (compare 327 the second and third lines in Table 1). 328

In the second set of simulations, the test for temporal variation rejected the null hypothesis in more than 90% when $\mu = 0$ and λ varied, whether this

was an increase or a decrease (third to sixth lines in Table 2). On the other 331 hand, the results were contrasted when $\mu > 0$. When there was no temporal 332 variation in the parameters, the type I error rates were inflated in relation 333 to the value of μ (seventh and eighth lines in Table 2). When μ varied 334 through time, the test behaved very differently depending on the direction 335 of this variation: it did not reject the null hypothesis in most cases when 336 μ increased (nineth line in Table 2) while it rejected it in 68% of the cases 337 when μ decreased (tenth line in Table 2). To further investigate this point, 338 we repeated some of these simulations but this time the null model was a 339 birth-death model with λ and μ constant through time, and the alternative 340 model was with λ constant and μ allowed to vary before and after 30 time 341 units. In this situation, the test behaved as expected: the rejection rate 342 was less than 5% when μ was constant, whereas it varied between 8% and 343 31% when the null hypothesis was false (Table 3). It is noteworthy that the 344 present test to detect time-dependent extinction rate is not very powerful: it 345 was necessary to simulate a strong contrast in μ to reach a statistical power 346 greater than 0.2. 347

The third set of simulations showed that the mixture-based LRT was able to detect heterogeneous diversification among two unknown categories of clades (Table 4). The test was more powerful when the contrast was due to different λ compared to different μ . Otherwise, the test showed satisfactory statistical performance: its power increased with sample size and/or contrast in the parameters.

The distribution of the estimates of speciation rate under the Yule model, $\hat{\lambda}_{Yule}$, shows that this estimator appeared unbiased when $\mu = 0$ (Fig. 1A). On the other hand, when $\mu > 0$ it was negatively biased though it can be observed that $\hat{\lambda}_{Yule} > \lambda - \mu$ so this cannot be actually taken as an estimator of the net diversification rate. The estimator based on the birth-death model, $\hat{\lambda}_{BD}$, appears less biased, even though the presence of extinctions seems to induce a slightly more dispersed distribution of the estimates (Fig. 1B). The estimates of extinction rate based on the birth-death model, $\hat{\mu}_{BD}$, were almost unbiased (Fig. 1C).

363 Application to Fish Data

The fit of the Yule model to the fish data at the higher level (N = 22)364 resulted in a global estimate $\hat{\lambda}_{\text{Yule}} = 0.058$ (SE = 0.002; AIC = 456). We 365 tried to fit a birth-death model which led to a much improved fit (AIC =366 376); however, the likelihood function had a pronounced ridge on the line 367 $\lambda = \mu$ (not shown). The fit of mixtures of Yule models with increasing 368 number of categories (K) showed that the best fit was with three categories 369 (Table 5). The parameter estimates were: $\hat{\lambda}_1 = 0.041, \ \hat{\lambda}_2 = 0.080, \ \hat{\lambda}_3 =$ 370 0.013, $\hat{f}_1 = 0.65$, and $\hat{f}_2 = 0.10$. The analysis of the combined taxonomic 371 and phylogenetic data (Paradis 2003) gave $\hat{\lambda} = 0.056$ and $\hat{\mu} = 1.83 \times 10^{-7}$. 372 The analysis at the level of the families (N = 97) gave for the Yule 373 model $\hat{\lambda}_{\text{Yule}} = 0.0756$ (SE = 0.0016; AIC = 1483). Like above, the fit of 374 the birth-death model resulted in a likelihood surface with a ridge on the 375 line $\lambda = \mu$. The mixture of Yule models with the best fit had two categories 376 (Table 5); the parameter estimates were: $\hat{\lambda}_1 = 0.099$, $\hat{\lambda}_2 = 0.036$, $\hat{f} = 0.42$. 377 The analysis with a model assuming continuous variation in λ across 378 clades gave close results for both taxonomic levels. In both cases, the model 379 fitted well and the AIC values were smaller than for any of the previous 380 models (Table 6). Figure 2 shows the distribution of λ inferred with the 381

estimated parameters. Trying to introduce μ did not result in successful fits and the estimates of this parameter were close to zero.

Vega and Wiens (2012) reported the percentage of marine and freshwater 384 species at both taxonomic levels. This was distributed very asymmetrically 385 with most orders and families having only marine or freshwater species. 386 Thus, we split the data into two groups whether they had more or less 387 than 50% of marine species. A test of different speciation rates between 388 these groups was performed. For orders, the difference was significant (LRT: 389 $\chi_1^2 = 28.09, P < 0.001$) with a larger estimate for marine orders ($\hat{\lambda} = 0.063$, 390 SE = 0.002) compared to the freshwater ones ($\hat{\lambda} = 0.046$, SE = 0.002). 391 An examination of the data suggested that this result was dependent on 392 Percomorpha which is one of the youngest clades in this data set and includes 393 16,625 species (Fig. 3A). Removing this clade resulted in a non-significant 394 test ($\chi_1^2 = 2.10, P = 0.147, N = 21$). For families, an analogous result 395 was found with a significant test (LRT: $\chi_1^2 = 5.58$, P = 0.018) comparing 396 marine families ($\hat{\lambda} = 0.079$, SE = 0.002) and freshwater ones ($\hat{\lambda} = 0.071$, 397 SE = 0.002). This result was dependent on two families older than 200 Myr 398 (Fig. 3B): the Amiidae (one species) and Polypteridae (12). Removing these 390 two families led to a non-significant test: $\chi_1^2 = 2.02, P = 0.155 (N = 95).$ 400

401 Discussion

The analysis of phylogenetic diversification with molecular data is enjoying a remarkable success in the literature. Some spectacular results have been accomplished using complete phylogenies (e.g., Goldberg et al. 2010; Hugall and Stuart-Fox 2012; Penney et al. 2012). Though complete phylogenies, possibly supplemented with fossil data, are probably the best way to investigate evolutionary diversification, the goal of our study was to show the merit of an alternative approach based on the analysis of clade data.

409 Our modeling approach is based on the assumption that each clade is

characterized by its diversification parameters and variation among these pa-410 rameters can be quantified in a statistical way. Bokma (2003) and Paradis 411 (2003) developed a method to combine information from high-level phylo-412 genies with clade data: both authors considered the simple constant-rate 413 birth-death model. Alfaro et al. (2009) used similar combined data to as-414 sess variation among clades of vertebrates using a stepwise procedure (see 415 details in Paradis 2012a). Thus the approach in the present paper comple-416 ments previous methodological developments. The possibility to quantify 417 variation among clades with linear models seems a fruitful way to avoid 418 overparameterization. Future applications will reinforce the relative merits 419 of this approach. 420

Recently, Stadler and Bokma (2013) developed alternative likelihood functions with respect to the way higher taxa are defined. They showed that the estimation of speciation and extinction rates vary substantially depending on these definitions. While they considered only the constant-rate birth-death model, it seems possible and interesting to include their sampling scheme into the developments presented in the present paper.

Our modeling approach ignores the background phylogeny of the clades, 427 the set of branches that link the clades together to make a higher-level 428 phylogeny. There are two reasons for this. First, using information from 429 the background phylogeny is straightforward when the rates of speciation 430 and extinction are constant and homogenous, but when this assumption 431 is relaxed it is not simple how one must assume changes in rates in the 432 background tree. It is clear that if a well-supported background phylogeny 433 is available, this might give additional information which can be combined 434 with clade data (e.g., Paradis 2003). However, this extra information will 435 in most cases require its own model since it relates to older diversification 436

events compared to clade data. On the other hand, ignoring backbone phy-437 logeny and assuming that the clades are independent units simplifies the 438 definition of alternative models as done in this paper. Second, though some 439 higher-level phylogenies are available (mammals, birds), we believe these are 440 still exceptions rather than the rule. For instance, the basal relationships 441 of reptiles, amphibians, or fishes are still debated. Therefore, having the 442 possibility to analyze their clade data without the need of a background 443 phylogeny is of some general application. Furthermore, the present ap-444 proach can be used when analyzing sets of clades across different phyla, for 445 instance arthropods, echinoderms, vertabrates, etc., where the background 446 phylogeny would not be very informative since this would branch at the 447 origin of Metazoa. 448

The use of mixtures as an approach to analyze heterogeneity in diver-449 sification rates is not limited to clade data. For instance, one could model 450 speciation and extinction rates on a fully-resolved phylogeny assuming that 451 these parameters vary among its branches though we do not know a pri-452 ori which sections of the tree evolved fast and which others evolved slowly. 453 Furthermore, the mixture approach can also be used to model variation in 454 rates of trait evolution along a phylogeny. In that case, the variation may be 455 among branches (as in the previous example), or among traits where some 456 traits are assumed to evolve faster but we do not know which ones. 457

Some subtle but important facts come from the results of the simulation study. Even though most of the tests considered here assumed $\mu = 0$, they appeared not to be tests of equal diversification. If the net diversification rates $(\lambda - \mu)$ were equal among clades, the tests rejected the null hypothesis in more than 5% (see eighth row of Table 1). On the other hand, if λ was equal among clades, the tests detected differences in μ . It is clear that results ⁴⁶⁴ based only on the Yule model must be interpreted with caution.

465 The tests of temporal variation showed some contrasted but interesting results. When the extinction rate was zero, these tests performed very well 466 and were able to detect either a decrease or an increase in speciation rate. 467 However, when extinction rate was not null, the tests based on the Yule 468 model showed poor performance with an increased type I error rate and a 469 high type II error rate (frequency of accepting the null hypothesis when it is 470 false) when μ decreased through time. These poor performances were cor-471 rected if the assumption $\mu = 0$ was relaxed (i.e., if a null birth-death model 472 was used in place of the Yule one), though the test had low power. Some 473 of these results make sense: the increased type I error rate obtained with 474 the Yule model is clearly due to the fact that a pattern of accelerated spe-475 ciation can be created under a diversification process with extinction, when 476 old lineages are mostly extinct (e.g., Paradis 2011). On the other hand, the 477 high type II error rate of the same model when extinction rate increased 478 through time is somehow surprising considering the widely reported results 479 of slowing-down diversification (Rabosky and Lovette 2008b,a; Morlon et al. 480 2011; Etienne and Haegeman 2012, among others). Obviously, the same test 481 was not used in these studies, so this clearly requires further investigation. 482 Besides, the result that the test based on a birth-death model shows statis-483 tically consistent results (i.e., the null hypothesis was rejected in less than 484 5% when μ was constant and in more than 5% when this parameter varied 485 through time) is encouraging and will also be further investigated. Interest-486 ingly, this test was more powerful when the extinction rate increased through 487 time. 488

A particularly interesting result comes from the precision of the estimator of extinction rate, $\hat{\mu}_{BD}$, which appears to have a very small bias, even when the data were simulated with a relatively large value of μ . This contrasts with previous studies showing that the estimator of extinction rate based on complete phylogenies is, overall, inaccurate except if it is small compared to the speciation rate (Paradis 2004; Didier et al. 2012). This result is important because several authors have cast doubt on the possibility to estimate with some precision extinction rates without fossils (Paradis 2011; Aldous et al. 2011).

The analysis with the fish data were essentially illustrative, but the re-498 sults call for several comments. The present method seems successful in 499 quantifying variation in diversification rates from a sample of clades. The 500 difference in the results from both taxonomic levels makes sense since we 501 expect more variation among families than among orders. The AIC values 502 evidence that the model assuming continuous variation in λ across clades 503 fits better than a model with discrete variation in this parameter. Since 504 similar tests have not been done with other data, this clearly calls for fur-505 ther analyses before concluding whether diversification varies continuously 506 or discretely across clades. 507

The apparent failure to estimate the extinction rate, μ , of fishes is disap-508 pointing since our simulation study showed that this parameter can be es-509 timated correctly with the present approach. The fossil record shows many 510 episodes of radiations, extinctions, and turn-over during the evolutionary 511 history of fishes (Friedman and Sallan 2012). So the reality is very differ-512 ent from the homogeneous scenario used in our simulations. Our results 513 combined with previous studies (e.g., Aldous et al. 2011) suggest that the 514 estimators of μ are far more complex when rate heterogeneity is present 515 which is likely the case with most real data set. 516

517

Vega and Wiens (2012) addressed the paradox of equivalent species di-

versity between marine and freshwater fishes despite the fact that freshwater 518 environments occupy a considerably smaller fraction of the Earth's surface 519 than oceans. In particular they wondered whether this could be related to 520 differences in diversification rates. Our results are in agreement with these 521 authors' who tested their hypothesis by correlating the proportion of marine 522 species in a clade with the method-of-moment estimator from Magallón and 523 Sanderson (2001). We found significant differences in λ between marine and 524 freshwater clades from the raw data; however, the small difference in λ be-525 tween both groups suggested the influence of one or two clades. Hopefully, 526 the analysis of a more comprehensive data set with the statistical tools intro-527 duced in this paper will help to solve the paradox of less biological diversity 528 in the ocean (Mora et al. 2011). 529

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λ_1	μ_1	λ_2	μ_2			n_1		
				1	3	5	10	20
0.1	0	0.1	0	0.044	0.060	0.066	0.054	0.056
0.1	0	0.1	0.05	0.038	0.085	0.108	0.140	0.203
0.15	0	0.1	0	0.094	0.177	0.232	0.418	0.711
0.15	0	0.1	0.05	0.112	0.297	0.446	0.759	0.958
0.2	0	0.1	0	0.174	0.497	0.707	0.943	0.998
0.2	0	0.1	0.05	0.236	0.643	0.855	0.993	1.000
0.1	0.05	0.1	0.05	0.040	0.054	0.048	0.054	0.061
0.15	0.05	0.1	0	0.050	0.075	0.083	0.123	0.209
0.15	0.05	0.1	0.05	0.069	0.129	0.201	0.387	0.653
0.2	0.05	0.1	0	0.119	0.240	0.384	0.693	0.928
0.2	0.05	0.1	0.05	0.143	0.407	0.618	0.878	0.995

Table 1. Rejection rate for the test of equality of diversification rate between two categories with n_1 and n_2 (= n_1) clades.

Table 2. Rejection rate for the test of temporal variation in diversification. The null model was a Yule model with constant rate, and the alternative model was a Yule model with λ allowed to take different values before and after 30 time units. The first two pairs of columns give the parameter values used for the simulations (Ancient and Recent: values before and after 30 time units).

An	Ancient		cent	Rejection rate
λ	μ	λ	μ	-
0.01	0	0.01	0	0.029
0.1	0	0.1	0	0.038
0.1	0	0.05	0	0.917
0.1	0	0.01	0	1.000
0.05	0	0.1	0	0.923
0.01	0	0.1	0	1.000
0.1	0.025	0.1	0.025	0.105
0.1	0.05	0.1	0.05	0.248
0.1	0.025	0.1	0.075	0.057
0.1	0.075	0.1	0.025	0.682

Table 3. Same than in Table 2 but the null model was a birth-death model with constant rates, and the alternative model was a model with λ constant and μ allowed to take different values before and <u>after 30 time units</u>.

Ancient		Re	ecent	Rejection rate
λ	μ	λ	μ	-
0.1	0.05	0.1	0.05	0.019
0.1	0.075	0.1	0.025	0.080
0.1	0.025	0.1	0.075	0.121
0.1	0	0.1	0.08	0.313
0.1	0.08	0.1	0	0.211

Table 4. Rejection rate for the test of equality of diversification rate between two unknowncategories using mixtures with n clades in each category.

λ	μ		n	
		10	20	50
0.1	0	0.011	0.006	0.011
(0.1, 0.2)	0	0.235	0.548	0.929
0.2	(0, 0.1)	0.057	0.143	0.369
0.2	(0, 0.15)	0.199	0.423	0.829

30	ven.							
	K	Orders			Families			
		$\ln L$	AIC		$\ln L$	AIC	_	
	2	-171.207	348.414		-599.846	1205.691		
	3	-158.381	326.763		-599.846	1209.691		
	4	-171.207	356.414		-599.846	1213.691		
	5	-171.207	360.414		-599.846	1217.691		
	6	-171.207	364.414		-599.846	1221.691		
	7	-171.207	368.414		-599.846	1225.691		

Table 5. Results of fitting models to the fish data using mixtures of Yule processes with Kfrom two to seven.

Table 6. Results of fitting a model of continuous variation in speciation rate across orders (N = 22) and families (N = 97) of fish.

Orders 3 Families 11	320.396 137.066	$\begin{array}{c} 1.221 \ (0.039) \\ 1.086 \ (0.026) \end{array}$	$\begin{array}{c} 0.163 \ (0.032) \\ 0.224 \ (0.022) \end{array}$



Figure 1. Distribution of the estimates of λ and μ with (A) the Yule model ($\hat{\lambda}_{Yule}$) and (B and C) the birth-death model ($\hat{\lambda}_{BD}$ and $\hat{\mu}_{BD}$) under five sets of parameters (values are given in the strips). Note the different scales of the *x*-axes. The vertical dotted lines indicate the values of λ (A and B) or μ (C) used in the simulation (not visible if outside the range of the *x*-axis). In all cases n = 100 clades.

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Figure 2. Inferred distribution of speciation rate among orders and families of fish.



Figure 3. Number of species with respect to stem clade age for (A) orders and some superorders and (B) families of fish (the legend is the same for both plots).